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# Assessment of mechanical property gradients after impact-based surface treatment: application to pure $\alpha$ -iron

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Mechanical surface treatments are known for their ability to improve material resistance to abrasive wear and local fatigue crack microstructure of the home-made crack propagation. These treatments are based on repeated contact loadings which create large plastic strains in the near-surface that can induce a local grain refinement. In this case, a significant increase in the near-surface local mechanical properties is thus usually observed. In this paper, nano-mechanical tests are used to quantify the mechanical property gradient in the near-surface of a purity-controlled  $\alpha$ -iron after an impact-based treatment. A methodology based on the combination of two different techniques is proposed: nano-indentation and in-situ micro-pillar compression. The resulting in-depth mechanical properties gradient is compared to the average grain size measured by EBSD. A positive relationship with the well-known Hall-Petch effect is observed.

## 1. Introduction

Surface mechanical treatments are used increasingly to maximize the lifetime of engineering parts by altering the near-surface mechanical properties. These treatments are based on repeated contact loading [1–3]. On the one hand, this can result in the creation of a local residual stress field which can prevent fatigue crack propagation, while on the other hand severe plastic deformation can occur in the near-surface which can lead to local microstructure transformation [4;5]. The latter is characterized by a progressive grain size refinement and consequently the formation of a mechanical property gradient over a few tens of microns [6]. The hardening of the near-surface is closely associated with an increase in grain boundary and dislocation density. The resulting ultra-fine grain zone is usually called a tribologically transformed surface (TTS) [7;8]. Beneficial physical properties such as high hardness and improved tribological properties are generally exhibited in these mechanically-induced transformed surfaces. The understanding of these surface mechanical treatments requires

the development of adapted characterization methods to accurately measure micro-structural and local mechanical properties, which is important as strong variation in-depth properties may appear because of microstructural gradients.

Two types of testing approaches for such measurements are nano-indentation and micro-compression [9,10]. While nano-indentation testing appears to be one of the best methods to reach this goal, data analysis remains a non-trivial task due to the well-known problem of contact area determination under load. It is thus difficult to obtain stress-strain curves at the length scale of the surface treatment, although this is of primary interest to engineers, especially for modeling purposes [9]. In contrast, micro-pillar compression tests could be a more direct method to accurately measure local stress-strain curves and obtain the mechanical property gradients in-depth. Nevertheless, the micro-pillar fabrication process in polycrystalline zones is a heavily laborious task [10], and is inherently difficult to translate to industrial purposes.

The main aim of this paper is to propose a new methodology based on the combination of nano-indentation and in situ micro-pillar compression for the assessment of micromechanical

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properties. In the past, several authors have independently used both of these techniques to identify the mechanical property gradient induced by surface treatments (SMAT, sliding deformation, shot-peening, etc.) in metallic materials [11–13]. Nano-indentation testing enables an overall measurement of the mechanical property gradient, while micro-pillar compression allows for an accurate quantification of the local stress-strain curves. Combining these two measurements, it is possible to obtain the yield stress as a function of distance to the surface assuming nano-hardness as three times the yield stress (for 8% of plastic strain) as proposed by Tabor [14–16].

The clear advantage of using both techniques is the possibility to compare two different kinds of measurements, allowing for local direct estimations (micro-compression) with a large testing coverage (nano-indentation) throughout the entire transformed region. Moreover, this combined procedure permits the investigation of some metallurgical effects involved in the surface strengthening, and associate them to the mechanisms governing the microstructural transformations. In other words, this work allows for the comprehension of the influence of surface mechanical treatments through quantification of the local mechanical properties.

This combined strategy is applied to a model material (pure iron), previously submitted to a nano-peening<sup>®</sup> treatment (impact-based treatment). The microstructure of the transformed zone, as well as the statistical analysis of the grain size distribution on the cross-section of the sample is first presented. Next, the methodology discussed above is applied to quantify the mechanical properties of the transformed zone. A relationship between the hardness gradient and the local microstructure is finally established, as well as a comparison between the properties measured by both techniques.

## 2. Process and methods: microstructural refinement on pure $\alpha$ -iron

### 2.1. Material

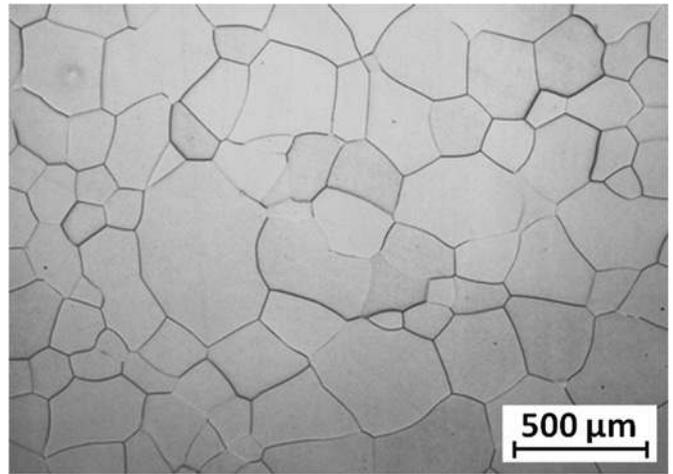
The mechanical surface treatment is carried out on a high-purity  $\alpha$ -iron produced using the cold crucible melting method. This enables the formation of  $\alpha$ -iron with less than 15 ppm of carbon. The metallic bar is treated thermo-mechanically (forging, annealing at 650 °C for 60 min) before applying the surface mechanical treatment. The resulting microstructure is shown in Fig. 1. Grains are equiaxed with an average grain size of approximately 250  $\mu\text{m}$ . No inclusions were observed. The sample surface was then mechanically polished with diamond suspensions of 3  $\mu\text{m}$  and 1  $\mu\text{m}$ .

### 2.2. Impact-based surface treatment: Nano-Peening<sup>®</sup>

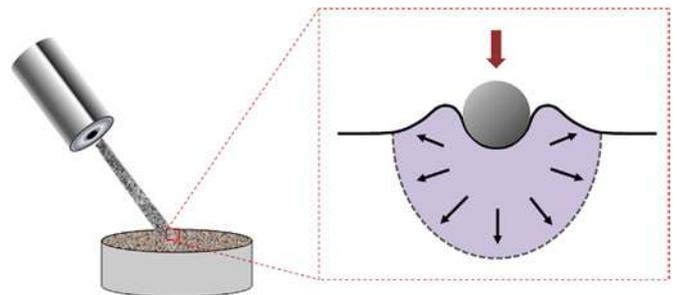
Nano-Peening<sup>®</sup> is a surface mechanical treatment developed by Winoa group (Fig. 2). Steel balls (0.1–2 mm diameter) are repeatedly projected towards the sample surface with an impact tilt between 10° and 45° at high speeds (40–100 m/s) [17;18]. Here, a surface coverage of 5000% has been used. This cold-working treatment is known to lead to severe plastic deformation of the near-surface and thus to grain refinement.

### 2.3. Microstructural characterization

Microstructural characterization was performed on material cross-sections using back-scattering electron microscopy in a Zeiss Supra 55 VP at 20 kV. Electron back-scattered diffraction (EBSD) mapping was obtained using a JEOL JSM-6500F at 20 kV and an



**Fig. 1.** Initial microstructure of the home-made purity-controlled  $\alpha$ -iron (15 ppm of carbon). Grains are homogeneous and equiaxed with an average grain size of  $\sim 250 \mu\text{m}$ .



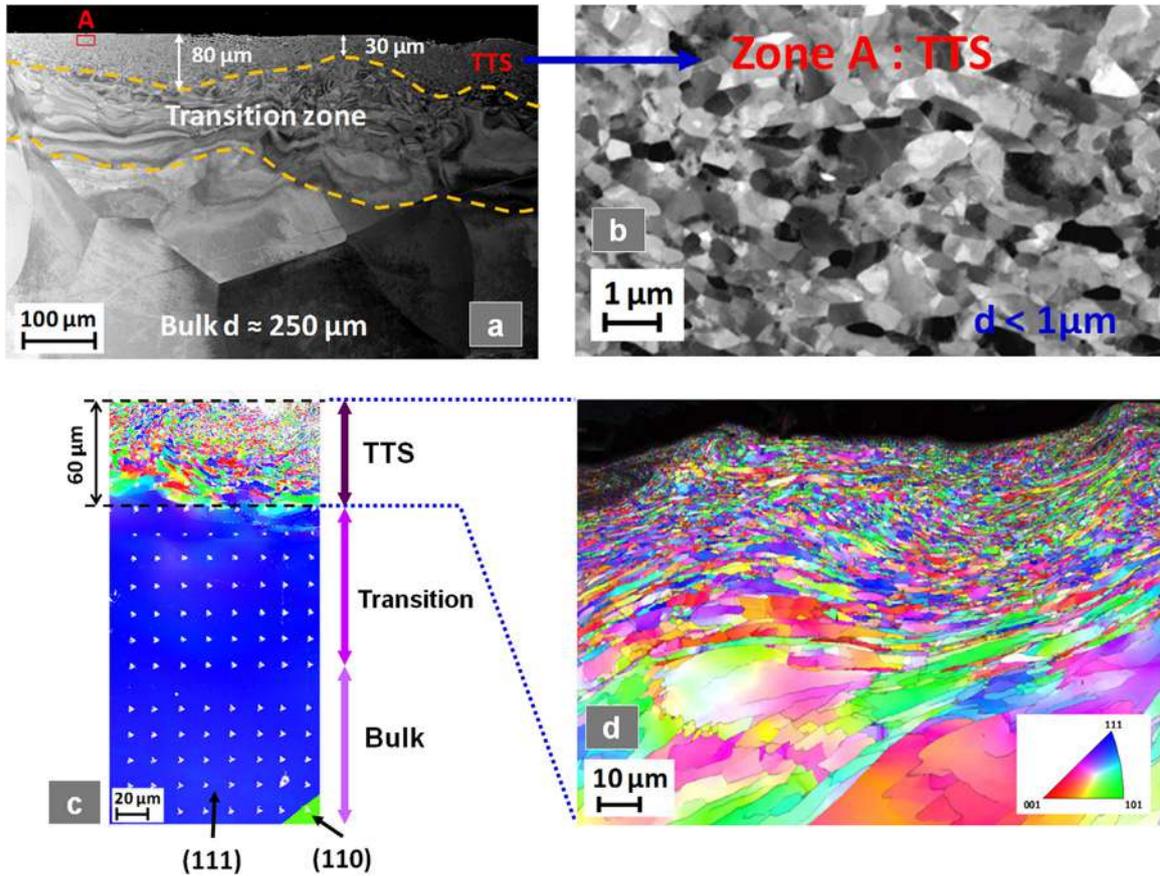
**Fig. 2.** Impact-based surface treatment: Nano-Peening<sup>®</sup>.

indexation step size of 0.3  $\mu\text{m}$ . Note that this step size was chosen to limit indexation drifts and have a reasonable acquisition time. Cross-sections were prepared using mechanical polishing until a diamond suspension size of 1  $\mu\text{m}$ . Surface finishing was carried out using colloidal silica.

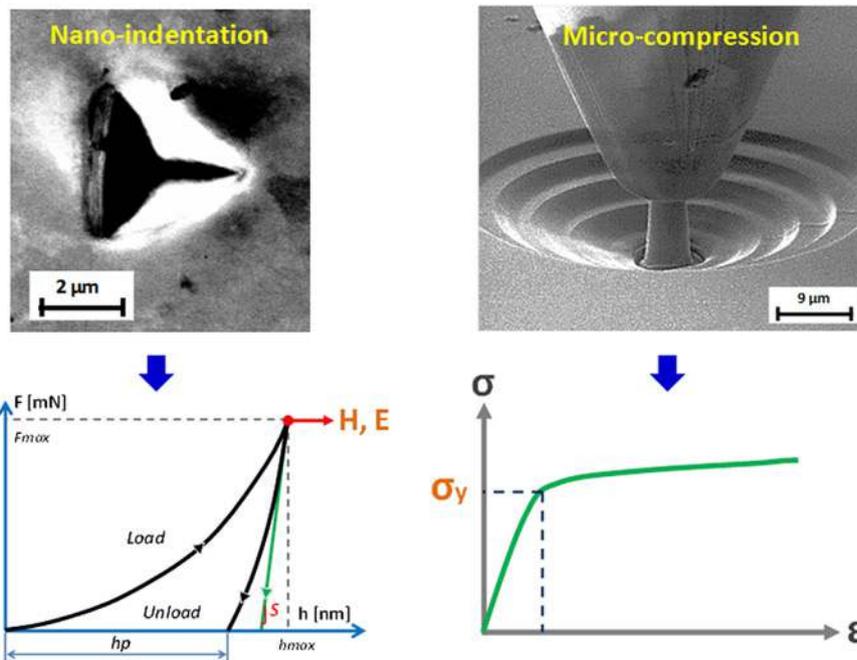
Three different regions can be clearly identified in the treated surface (Fig. 3a and c). The first zone corresponds to a tribologically transformed surface (TTS) composed of well-defined sub-micrometric grains (Fig. 3b and d). The thickness of this zone varies from 30  $\mu\text{m}$  to 80  $\mu\text{m}$  with an average value of 50  $\mu\text{m}$ . The TTS region is composed of grains with sizes predominately below 1  $\mu\text{m}$  diameter with various crystal orientations. This refined microstructure is followed by a transition zone, where no new grains are formed in spite of the severe deformation and crystal misorientation [19]. Finally the third zone corresponds to the initial bulk material without microstructural transformation (as shown in Fig. 1).

### 2.4. Measurement of mechanical properties by nano-mechanical testing

The grain size decrease and the microstructural gradient are closely related to the change in mechanical properties from the near-surface to the inner bulk material. Two different nano-mechanical testing techniques are employed to quantify this gradual variation on the mechanical behavior: nano-indentation and micro-compression (Fig. 4). Nano-indentation permits the estimation of the hardness (H) and Young's modulus (E) from the maximal load point of the indentation curve (as outlined in Fig. 4). In contrast, the micro-pillar compression test leads to the measurement of true stress-strain behavior, discounting for



**Fig. 3.** Characterization of the microstructural transformed surface after shot-peening treatment on pure  $\alpha$ -iron: global view of the cross-section by (a) BSE and (c) EBSD map; local view by (b) BSE and (d) EBSD map. Note that the small white spots in figure (c) correspond to nano-indentation prints.



**Fig. 4.** Nano-mechanical testing used on the quantification of mechanical property gradients produced by shot-peening treatment on  $\alpha$ -iron. Note that mechanical properties, hardness (H) and elastic modulus (E), are obtained from nano-indentation testing at the maximal load point of the force-displacement curve.

strains lower than a few percent where uncertainties in compression direction and the pillar surface roughness make precise measurement of elastic properties difficult.

#### 2.4.1. Nano-indentation testing

Nanoindentation tests have been performed with an Anton Paar SA<sup>®</sup> NHT nanoindenter using a Berkovich tip. Tests were arranged in a rectangular grid matrix ( $10 \times 20$ ), with a  $15 \mu\text{m}$  spacing

between indents on both vertical and horizontal axes (Fig. 5a). Twenty different depths were investigated. A maximal force of 10 mN is applied with a load-unload rate of 20 mN/min. Hardness and elastic moduli are computed using the contact stiffness [20;22], which is measured as the initial slope of the unloading part of the force-displacement curve (Fig. 4) [23;24] using the Loubet's contact model [21]. Note that the distance between indentations (15  $\mu\text{m}$ ) is higher than three times the characteristic length of the residual imprints ( $\leq 4 \mu\text{m}$ ) to avoid perturbations due to the mechanically affected zone of adjacent tests (Fig. 5b and c) [25]. An indentation force of 10 mN permits the investigation of several positions in the TTS region without interfering with adjacent measurements. For comparative purposes, the same indentation force has been used throughout the whole cross-section.

#### 2.4.2. Micro-pillar compression

As for nano-indentation tests, micro-pillar compressions are performed over the cross-section. Two pillars are produced in the TTS and bulk regions as shown in Fig. 6a. These were milled using a gallium source of the Zeiss NVision40 focused ion beam (FIB) system. The fabrication process includes 3 rough milling phases and a final polishing step [26–28]. The gallium beam is used at 30 kV and the milling current ranges from 27 nA for rough milling to 700 pA for final polishing. This strategy allows for cleaner and more homogenous pillar surfaces to be obtained. The aspect ratios of the TTS and bulk pillars (Fig. 6b and c) are 2.6 (9.3  $\mu\text{m}$  diameter and 24  $\mu\text{m}$  height) and 1.9 (5.4  $\mu\text{m}$  diameter and 10.4  $\mu\text{m}$  height) respectively. The TTS pillar is located at a depth of 15  $\mu\text{m}$  from the surface, which corresponds to a polycrystalline material of ca. 800 nm average grain size. The polycrystalline pillar contains approximately 11 grains across the diameter. The bulk pillar was

produced in a grain with crystal orientation  $\langle 225 \rangle$  with respect to the load direction. Both pillars have a conical shape with a tapered angle of 2.5° and 4.5° for the TTS and bulk zones respectively. The compression tests were made in situ in a scanning electron microscope (SEM) with an Alemnis nano-indentation set-up [29]. Both compressions were carried out with a 15  $\mu\text{m}$  diameter flat punch at a load-unload rate of 0.03  $\mu\text{m/s}$ .

### 3. Results

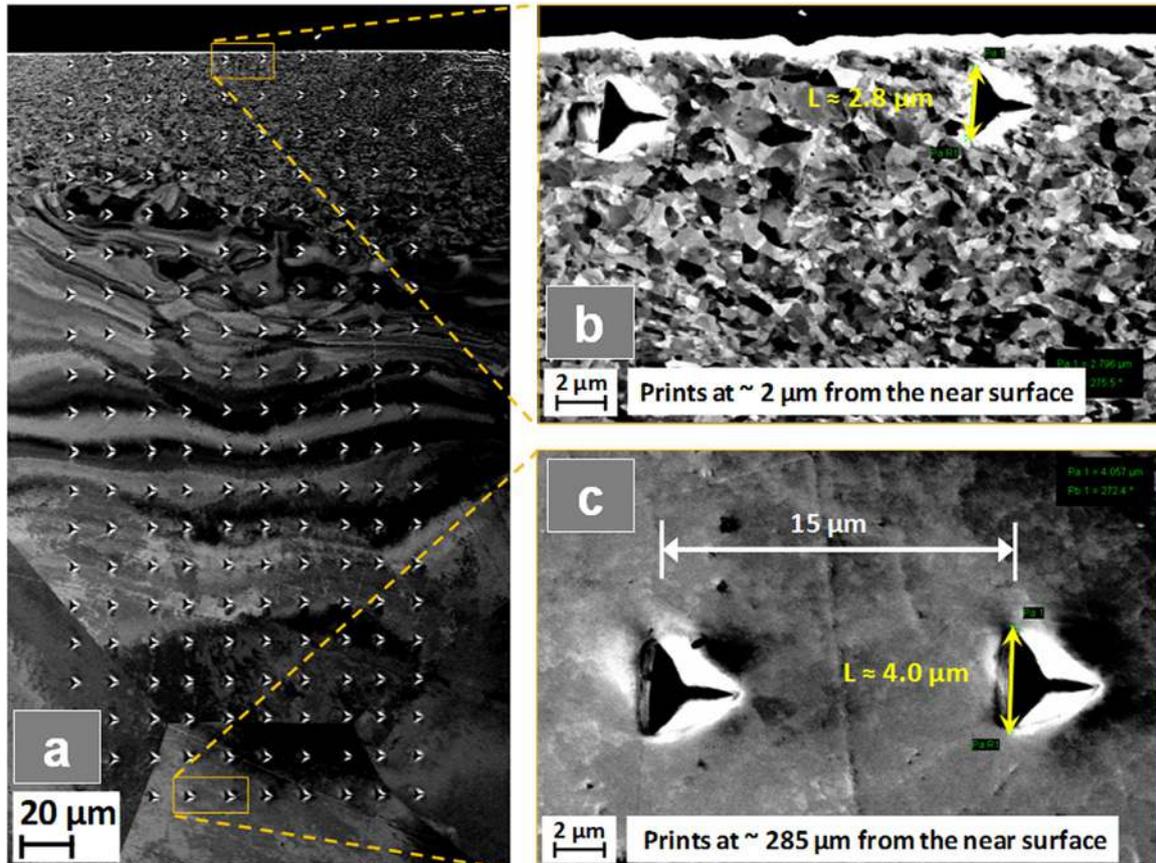
#### 3.1. Grain size distribution of the mechanically transformed surface

The average grain size was measured in the mechanically transformed surface from the EBSD map shown in Fig. 3c. It evolves from 0.76  $\mu\text{m}$  up to 5.82  $\mu\text{m}$  at the bottom limit of the TTS region, i.e. roughly 60  $\mu\text{m}$  from the surface (Fig. 7). It is important to note that the ratio between the grain size at the near-surface and the initial bulk grain dimensions is approximately 330.

Concerning the transition zone, the EBSD map as well as the SEM image (Fig. 3a and c) highlight the presence of considerable crystal misorientations produced by severe plastic deformation. However, the deformation level is not severe enough to promote the creation of new grain boundaries [19].

#### 3.2. Hardness gradient measured by nano-indentation testing

Arrays of residual imprints at two different depths are presented in Fig. 5b and c. The lateral dimensions are closely related to the microstructural evolution along the cross-section, highlighting the increase in mechanical properties for the near-surface.



**Fig. 5.** Indentation matrix (10 × 20) made on the cross section of the hyper-deformed surface (a), corresponding to the EBSD map used for estimate the grain size distribution. Indentations prints with 15  $\mu\text{m}$  spacing and a force of 10 mN with a Berkovich tip (b, c).

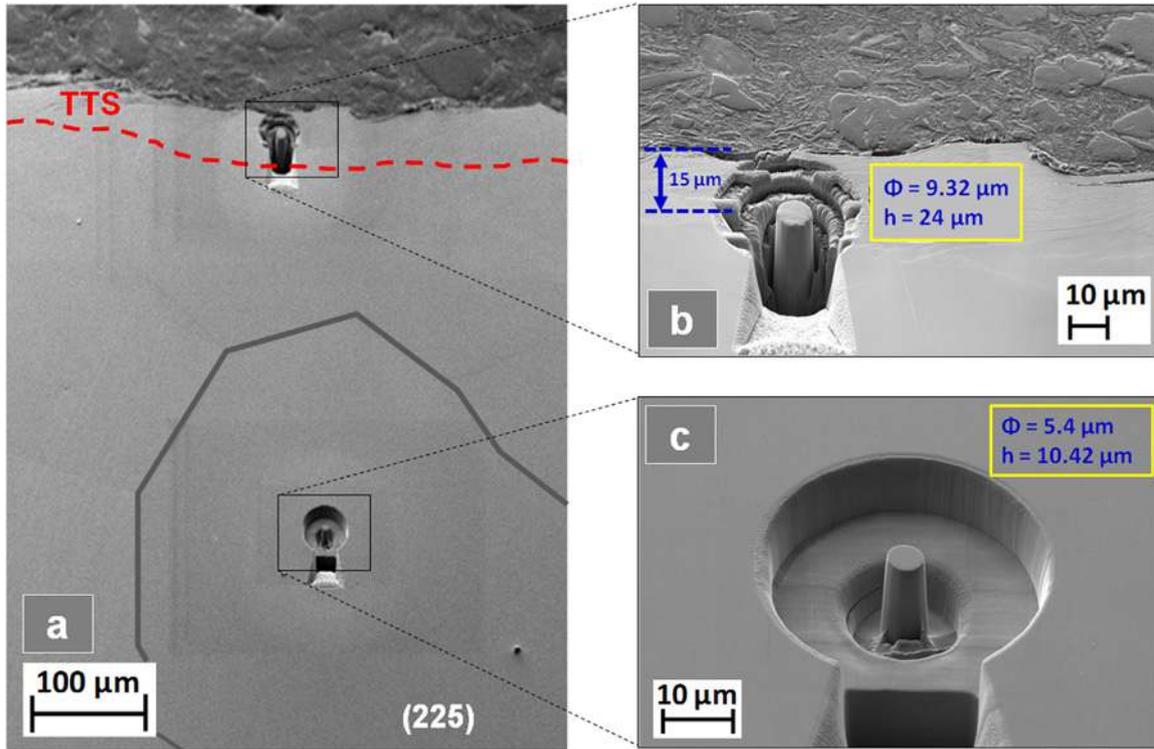


Fig. 6. (a) Micro-pillars position on the cross-section, (b) TTS micro-pillar and (c) bulk micro-pillar.

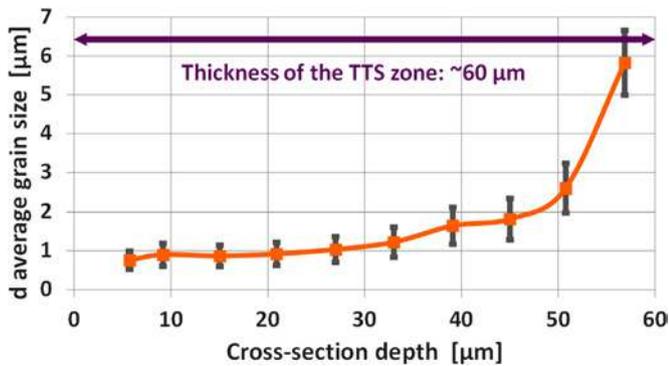


Fig. 7. Grain sizes distribution as a function of the cross-section depth in the TTS zone.

For instance, the characteristic size of the residual impression at ca. 2 μm depth is approximately 2.8 μm, contrary to the one located at ca. 285 μm from the surface where the length increases up to 4 μm. According to the EBSD map in Fig. 3c, the nano-indentation tests in the bulk material were predominately carried out for a  $\langle 111 \rangle$  crystal surface orientation.

The in-depth hardness and Young's modulus are plotted in Fig. 8a and b. In both curves, each point corresponds to the average value obtained from the ten indentation tests carried out at each depth. The measurements performed at 2 μm from the surface, corresponding to the first point of each curve, are mostly erroneous, and as such have not been taken into account. The average hardness decreases from 2300 MPa in the near-surface, to 1250 MPa at 150 μm depth (Fig. 8a). The hardness is therefore reduced by 40%, of which 30% corresponds to the first 60 μm of the TTS layer, followed by a 10% reduction over the transition zone. The plateau corresponds to the initial bulk material properties.

As expected, Young's modulus remains constant at ca. 207 GPa [23,30] over the entire cross-section. The elastic modulus represents the material atomic binding forces responding to an external load

[30], while several investigations have pointed out that the Young's modulus could vary in a material due to different reasons: temperature variations [31], material porosity [30], phase transformations [31] or crystallographic orientations. In this work, the homogeneous features of high-purity  $\alpha$ -iron as well as the multi-dimensional loading condition of indentation tests [32] could explain this low elastic modulus anisotropy, even in the presence of a significant grain size refinement and various crystal orientations.

### 3.3. Micro-compression test results

The results of in situ compression tests are presented in Fig. 9. It was observed that the TTS pillar deformation is entirely homogeneous (Fig. 9a-c), which is expected due to its polycrystalline nature. On the other hand, the pillar situated in the bulk of the sample deforms in a well-defined slip plane, as indicated by the white arrows in Fig. 9e and f. This kind of behavioral feature is typical of single crystals, due to the activation of a preferential slip system under mechanical loads [33].

True stress-strain curves are obtained from the force-displacement data of both micro-compression tests (Fig. 10). Compliance effects from the frame, substrate and indenter were subtracted from the measured force-displacement values during data processing. The yield strength estimated for the TTS and bulk regions were ca. 700 MPa and ca. 300 MPa respectively. Plastic flow was observed through an absence of strain hardening for the TTS pillar, whereas a slight strain-hardening was detected for the single-crystal pillar. Note that the initial yield strength is close to the yield stress at a strain of 8% ( $\sigma_{0.08}$ ), the representative strain related to Berkovich indentation [16,34], for both regions (TTS and bulk). It should be noted that micro-compression does not allow the measurement of initial yield stress with a very good accuracy for metals. Indeed, a very small difference between the compression direction and the pillar axis may prevent an accurate measurement of the elastic component for such materials. As an example, it can be seen that the Young's modulus which could be

measured from Fig. 10 would be significantly lower than the true Young's modulus of pure iron.

## 4. Discussion

### 4.1. Nano-indentation vs micro-compression

According to the curves presented in Figs. 8 and 10, high increments of mechanical properties were quantified using both

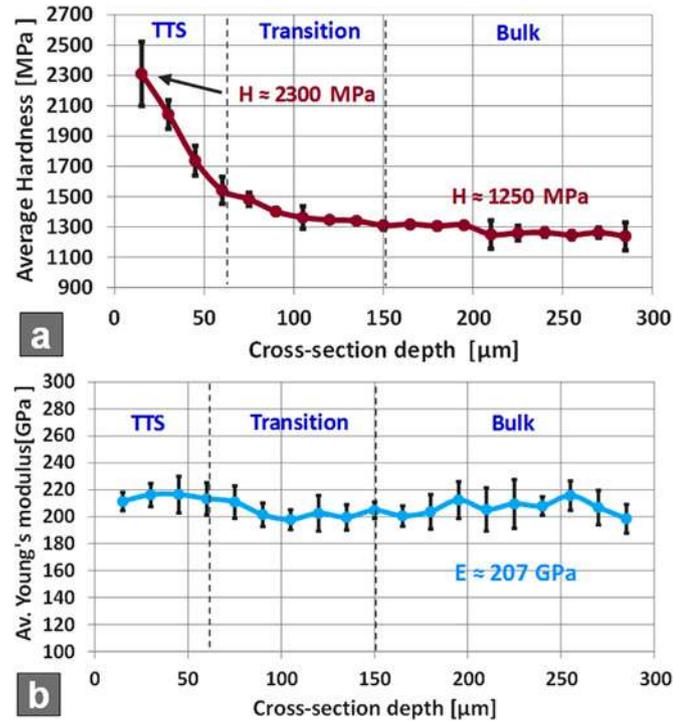


Fig. 8. Evolution of (a) average hardness [MPa] and (b) average Young's modulus [GPa] over the cross-section. Curves are estimated using the model of Loubet.

techniques. Micro-compression tests show that the yield strength of the TTS zone is approximately twice that measured in the bulk material region, which is closely related to the hardness gradient estimation (ca. 40%).

Furthermore, nano-indentation and micro-compression results can be compared within the context of the experimental Tabor relationship for metals [14,15], in which the hardness corresponds to approximately three times the yield strength for a representative strain of 0.08 ( $H/\sigma_{0.08} \approx 3$ ) [16]. The polycrystalline zone presents a ratio of ca. 3.3 (2300 MPa/700 MPa), meanwhile the bulk material region exhibits a ratio of ca. 4.2 (1250 MPa/300 MPa). The latter value deviates slightly from the expected ratio.

In a first approach, one can presume that the discrepancy between the measurements done by nano-mechanical testing in single crystal regions may be related to the different crystal orientations. More precisely, nano-indentation and micro-compression tests in the bulk material were carried out in  $\langle 111 \rangle$  and  $\langle 225 \rangle$  orientations, respectively. Considering the 48 possible slip systems for  $\alpha$ -iron (three kinds of plane and direction families for bcc crystal structures) [35], the maximal Schmid factors with respect to the normal direction of the surface for these two grains are  $m_{\langle 111 \rangle} = 0.314$  and  $m_{\langle 225 \rangle} = 0.433$ . Indeed, the indented bulk zone seems to be 1.38 times ( $m_{\langle 225 \rangle} / m_{\langle 111 \rangle}$ ) stronger than the compressed bulk zone, which appears to be consistent with the results above. However, this interpretation should be taken with caution as the multiaxial nature of nano-indentation loading in single crystals could activate several slip systems simultaneously [32].

As was previously presented by Vlassack and Nix [36], the hardness and elastic moduli of single crystals do not vary significantly with respect to the indentation orientation axis. In that work, the anisotropic behavior of single crystals with different orientations ( $\{100\}$ ;  $\{110\}$ ;  $\{111\}$ ) was presented for several cubic structure materials: copper,  $\beta$ -brass, aluminum and tungsten. From numerical simulations and experimental nano-indentation tests, they observed slight anisotropic variation in hardness (less than 13%) and indentation modulus (between 10% and 25%). It would suggest that multiple slip systems are activated during indentation [32,37] and the hardness measurement corresponds to the averaged behavior of all these glide systems. In other words,

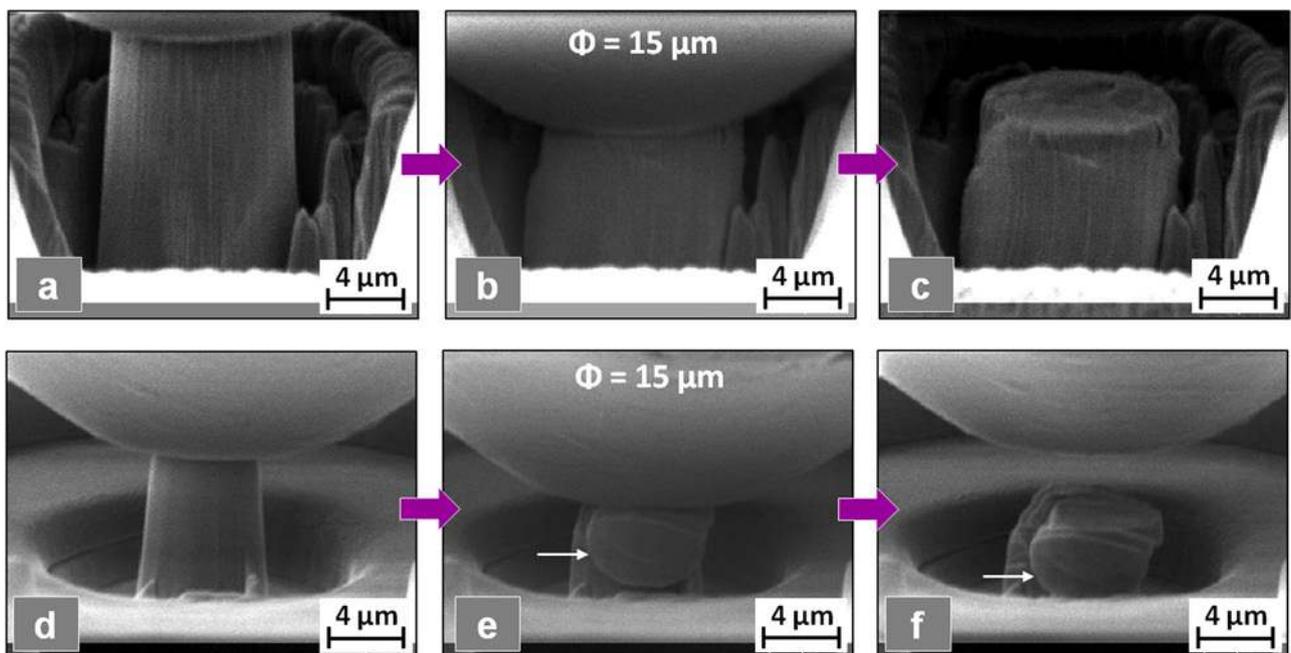


Fig. 9. Micro-pillar compression tests of the TTS region (a,b,c) and the bulk material (d,e,f), using a flat tip of  $\Phi$  15  $\mu$ m.

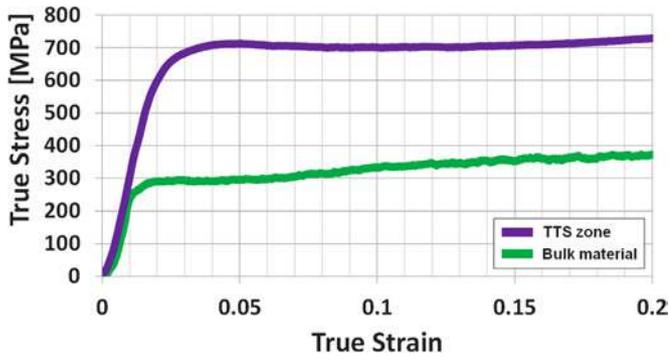


Fig. 10. True stress-strain curves of the TTS zone and bulk micro-pillars.

the hardness does not change so much with the crystal orientation in spite of the significant yield stress anisotropy that could exist in the material [36].

According to that, the difference between the mechanical properties quantified in single crystals is particularly related to the nature of the load and the corresponding plastic deformation effected. Indeed, it could be possible that hardness measurement values in single crystals are higher than those expected on the yield stress basis [36]. Due to the low anisotropy observed from nano-indentation testing, it would not be surprising if the hardness measurement in a  $\langle 225 \rangle$  indentation direction (same orientation as compression test) remains at ca. 1250 MPa. This is clearly visible from hardness measurements corresponding to the last two lines of indentation imprints in the rectangular array shown in Fig. 5-a. As shown in this figure, indentations were performed in other single crystal orientations (for example  $\langle 110 \rangle$ ) from the EBSD map in Fig. 3c) and the average hardness remains at approximately 1250 MPa (Fig. 8). Despite the mechanical property differences observed for single crystals in this work, it is noted that the Schmid factor remains a main criterion regarding the comparison between uni-axial load tests. Likewise, nano-mechanical tests were carried out near the transformed region and the influence of dislocation density, which has not been explicitly taken into account in this investigation, could also play a role.

Moreover, micro-compression tests reveal negligible strain hardening for the polycrystalline pillar, in contrast to the bulk material pillar behavior (Fig. 10). Due to the sub-micrometric grain sizes and the severe plastic deformation already introduced in the TTS zone, the pillar deformation could be mostly governed by grain boundary interactions [38] instead of dislocation interactions in the grains (Taylor's expression) [39]. Size effects are not taken into account as both pillars do not have sub-micrometric dimensions; a condition that is specified in literature [40–42].

#### 4.2. Hardness and grain size relationship: the Hall-Petch effect

The micro-structural transformation of pure  $\alpha$ -iron is closely related to its high stacking fault energy, allowing for favorable dislocation movement and migration [43]. In this material, grain refinement occurs essentially in three steps during severe plastic deformation [44,45]. Firstly, for low strain levels, dislocation glide exists in multiple slip planes and the material is arranged in cellular substructures subdivided by high-dislocation-density walls. In this first phase, low angle boundaries are created in the initial grains. Secondly, when the deformation increases up to middle strains, the dislocation sub-boundaries of these cell blocks become considerably misoriented. In this case, multiple micro-shear bands start appearing into the grains with various directions. Several micro-shear band interactions lead to high-angle boundaries dividing the original grains into small structural elements. Finally, there is a saturation of micro-shear bands and dislocation

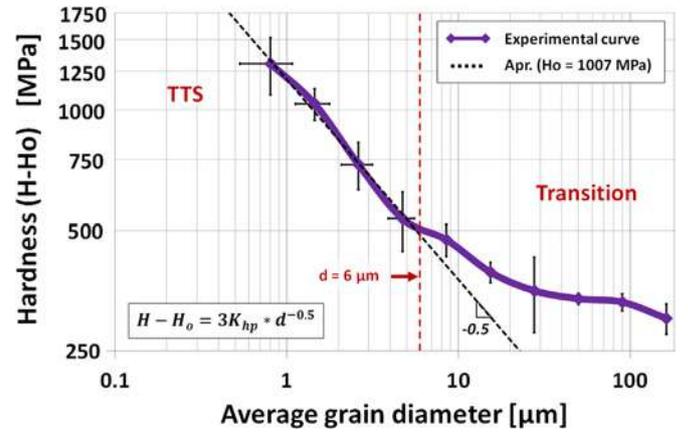


Fig. 11. Power law describing the relationship between the relative mean hardness ( $H-H_0$ ) and the average grain diameter ( $d$ ) on the micro-structured zone: Hall-Petch effect.

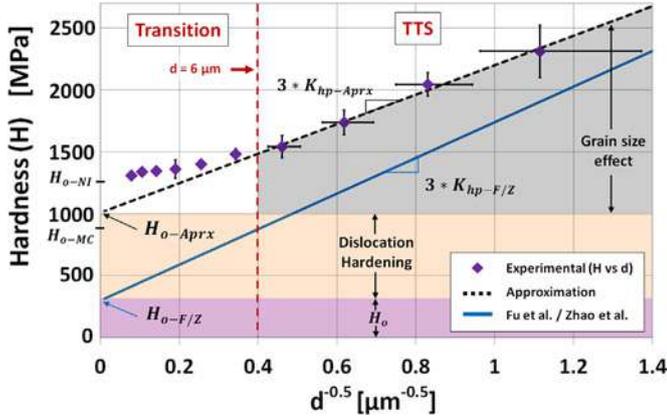
densities allowing for the formation of well-defined grains.

Considering the mechanisms governing this microstructural transformation, it is not surprising that the increase in mechanical properties is closely related to the increase in grain boundaries as well as the rise of local dislocation densities. Nano-indentation testing revealed that the hardness decreases approximately 40% over a 150  $\mu\text{m}$  depth, corresponding to the TTS and transition zones along the cross-section. It is therefore possible to correlate the quantified average hardness gradient with the grain size distribution obtained from the EBSD map (Fig. 11).

Fig. 11 shows that the hardness decreases linearly with the logarithm of the average grain size, which is consistent with microstructure refinement effects, such as the Hall-Petch effect. Once the average grain size goes beyond 6  $\mu\text{m}$ , i.e. at 60  $\mu\text{m}$  depth, the transition zone is reached and the linear tendency vanishes progressively. The grain size in the transition zone corresponds to an extrapolation of the grain size distribution in the TTS layer. As was mentioned in Section 2.3, grains along the transition zone are not well-defined and consequently the Hall-Petch relationship for that region can no longer be applied. As such, the decrease in hardness is likely related to the gradient of dislocation densities and the local misorientation [4,46], also associated with the presence of sub-grain boundaries.

In order to understand the Hall-Petch effect in the sub-micrometric region, the experimental curve in Fig. 11 is fit using the equation:  $H - H_0 = 3K_{hp}d^{-0.5}$ , where  $K_{hp}$  is a material constant,  $H_0$  is the bulk material hardness, and  $d$  is the grain diameter [47]. The obtained approximation (black dashed line in Fig. 11) corresponds to the following material constants:  $H_{0-Apprx} = 1007.8 \text{ MPa}$  and  $K_{hp-Apprx} = 397.15 \text{ MPa}\mu\text{m}^{0.5}$ .

The same experimental values are plot in Fig. 12 to compare the fitted approximation (black dashed line) with the linear Hall-Petch model proposed in literature for  $\alpha$ -iron (blue line). Both straight lines represent the equation  $H = H_0 + 3K_{hp}d^{-0.5}$ , where  $H_0$  is the intercept of the vertical axis and  $3K_{hp}$  is the slope of the line. The material constants used from literature (blue line) are  $K_{hp-F/Z} = 480 \text{ MPa}\mu\text{m}^{0.5}$  and  $H_{0-F/Z} = 300 \text{ MPa}$ , taken from Fu et al. [48] and Zhao et al. [49]. These authors suggest that the  $K_{hp}$  value could vary in pure  $\alpha$ -iron for different grain size ranges [48,49]. For micrometric grain diameters, the Hall-Petch effect is described by a typical linear relationship with a slope of  $480 \text{ MPa}\mu\text{m}^{0.5}$  [48]. When the average grain size approaches the nanocrystalline range ( $d < 100 \text{ nm}$ ), this linear tendency starts to disappear and the slope evolves continuously to  $210 \text{ MPa}\mu\text{m}^{0.5}$  [48]. Considering the grain size distribution of the TTS zone, the estimated material constant  $K_{hp-Apprx}$  ( $400 \text{ MPa}\mu\text{m}^{0.5}$ ) is in reasonable agreement with



**Fig. 12.** Comparison of the Hall-Petch effect identified from indentations tests (black dashed line) with models proposed by Fu et al. [48] and Zhao et al. [49] for pure  $\alpha$ -iron (blue continuous line). Straight lines represent the equation  $H = H_0 + 3K_{hp}d^{-0.5}$ , where  $H_0$  is the intercept of the vertical axis and  $3K_{hp}$  is the slope of the line. The Hall-Petch constants are:  $H_{0-Apprx} = 1007.8 \text{ MPa}$ ;  $K_{hp-Apprx} = 397.15 \text{ MPa}\mu\text{m}^{0.5}$  for the approximation and  $H_{0-F/Z} = 300 \text{ MPa}$ ,  $K_{hp-F/Z} = 480 \text{ MPa}\mu\text{m}^{0.5}$  for the model of Fu et al. and Zhao et al. Values of  $H_{0-NI}$  and  $H_{0-MC}$  are 1250 MPa and 900 MPa respectively. In this figure, purple dots correspond to the experimental data. Note that error bars are not visible in four dots of the transition zone due to the low standard deviation of these points (less than 27 MPa). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the value for the slope proposed in literature for micrometric ranges  $K_{hp-F/Z}$  ( $480 \text{ MPa}\mu\text{m}^{0.5}$ ) [48]. From Fig. 12, it is visible that the slopes of both straight lines are similar. This could suggest that the grain size effect quantified by nano-indentation tests in the TTS region is consistent with models already proposed in the literature for  $\alpha$ -iron. The discrepancy between these values is likely caused by a slope drop in the presence of a sub-micrometric grain range, as the indexation step size of the EBSD map ( $0.3 \mu\text{m}$ ) is not enough to reveal grains smaller than 500 nm in diameter at the near-surface.

The significant difference between both curves (Fig. 12) is the y-axis intercept of each straight line, i.e. the  $H_0$  value. This value represents the mechanical behavior associated with dislocation interactions and movements during plastic deformation. Some authors affirm that  $H_0$  corresponds to the combined effect of the Peierls stress and the work-hardening produced by an increase of dislocation density [50]. For pure  $\alpha$ -iron, the hardness related to the Peierls stress ( $H_p \approx 3\sigma_p = 334.2 \text{ MPa}$ ) [35] corresponds approximately to the material constant proposed in the model of Fu et al., ( $H_{0-F/Z} = 300 \text{ MPa}$ ) [48]. It would mean that the discrepancy between both constants ( $H_{0-Apprx}$  and  $H_{0-F/Z}$ ) is essentially related to the high strengthening level produced by severe plastic deformation during the shot-peening process. In Fig. 12 this corresponds to the "Dislocation Hardening" region, which represents the vertical rise of the straight blue line due to the increase of dislocation density. In other words, Fig. 12 shows the different effects involved in the material strengthening caused by the mechanical surface treatment and the micro-structural refinement. The first region ( $H_0$ ) represents the initial theoretical mechanical properties proposed in literature for a quasi-free dislocation  $\alpha$ -iron. The second zone (*Dislocation Hardening*) represents the increase of dislocation density due to severe plastic deformation. Note that the preexisting dislocation density state (or statistically stored dislocations, SSD) [51] of the material used in this work could also contribute to the hardness increase in this region. The last zone (*Grain size effect*) corresponds to the term  $3K_{hp}d^{-0.5}$  of the Hall-Petch equation. This zone is bounded by a grain size of  $6 \mu\text{m}$ , from where the transition zone starts and there are no longer well-defined grains.

It is interesting to observe that the estimated value of  $H_{0-Apprx}$  is between the bulk material constant measured with nano-indentation ( $H_{0-NI} \approx 1250 \text{ MPa}$ ) and the one quantified using the yield strength from micro-compression ( $H_{0-MC} \approx 3 * 300 \text{ MPa} = 900 \text{ MPa}$ ) [52,53]. The discrepancy between these values may be explained by several reasons. Firstly, as was presented in the previous section, the hardness measurement corresponds to an averaged behavior of various slip systems, and the anisotropy perceived from nano-indentation testing is less significant. For that reason, some literature suggests that hardness measurements in single crystals can take higher values than those expected on the yield stress basis [36]. Secondly, the different crystal orientations of the single crystal zones where nano-mechanical testing was performed ( $m_{\langle 111 \rangle} = 0.314$ ;  $m_{\langle 225 \rangle} = 0.433$ ) could enlarge the difference between both measurements. Moreover it could be possible that both nano-mechanical test zones did not have the same increase in dislocation density after the mechanical surface treatment. As was previously observed, the dislocation density has a significant influence on mechanical property characterization. While not within the scope of this paper, quantification of this effect could be performed using high resolution EBSD, and will be the aim of future work.

The last question arising concerns possible residual stress effects on the measurement of mechanical property gradients, relating to the microstructural evolution in the cross-section. As shown by several authors [54,55], residual stresses could confer a significant effect on nanoindentation results. However, the residual stress-free condition of the polycrystalline pillar and the good agreement between measurements in this region ( $H/\sigma_{0.08} \approx 3.3$ ) lead us to the conclusion that residual stress effects are effectively negligible when compared to microstructural factors. However, hardening induced by an increase in dislocation density can play a major role as was previously discussed. It is quite clear that addressing these two uncertainties could give more judicious interpretations for the determination of material constants ( $H_0$ ,  $K_{hp}$ ) in pure  $\alpha$ -iron.

## 5. Conclusions and perspectives

In this work, an innovative approach based on the combination of two types of nano-mechanical tests was used to quantify the mechanical property gradient induced in pure  $\alpha$ -iron by an impact-based surface mechanical treatment. The grain size refinement produced in the near-surface and its influence on the hardness and yield strength evolution was additionally considered.

Both mechanical tests showed clearly an increase in mechanical properties due to the mechanical surface treatment. The nano-indentation results are generally consistent with the micro-compression results. The experimental Tabor's relationship between hardness and yield strength was confirmed, revealing results consistent with the expected ratio ( $H/\sigma_{0.08} = 3$ ) classically used in literature [16,34], especially for tests carried out in polycrystalline regions.

The hardness gradient quantified by nano-indentation was closely related to the grain size distribution obtained from an EBSD map on the near-surface. The experimental data agrees with the theoretical Hall-Petch relationship, leading to the assessment of characteristic pure  $\alpha$ -iron constants ( $H_0$ ,  $K_{hp}$ ). The grain size effect observed in this work is consistent with several model parameters proposed in literature for pure  $\alpha$ -iron [48,49]. Based on this analysis, it is obvious that grain size refinement has a considerable influence on the increase of mechanical properties and the evolution of the material's mechanical behavior, along with the presumably significant influence of dislocation density increments due to severe plastic deformation. Quantification of this effect will

be the aim of future work.

Comparing both techniques, nano-indentation seems to be the less arduous method for the measurement of mechanical property gradients. However, data analysis and results are considerably dependent on the contact model used. On the other hand, micro-compression offers a direct way to estimate the material's local constitutive behavior law. Nevertheless, considering the laborious micro-pillar fabrication process in the polycrystalline region and the good agreement between both techniques, nano-indentation remains an advantageous method to qualify mechanical property gradients.

Furthermore, this paper highlights that pure iron is an appropriate model material for obtaining a well-defined TTS region in order to compare both techniques. Likewise, such a material is favorable for SEM imaging and EBSD mapping, as well as displaying good homogeneity for FIB fabrication processes.

Future work will investigate the correlation between micro-pillar compression curves and the representative stress-strain values obtained from nano-indentation tests [16,56]. Quantification of the mechanical property gradients presented in transformed surfaces induced by other kinds of contact loading treatment, as for high pressure torsion (HPT) [7,45] or micro-percussion tests [57,58] will also be addressed.

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