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# Morphological characterization of compact aggregates using image analysis and a geometrical stochastic 3D model

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**Abstract**—The 3D morphological characteristics of size and shape of latex nanoparticle aggregates have a major impact on the quality of these powders and their performances such as flowability/processability in an industrial context. Most of the time the morphological characterization of these aggregates is only possible from the analysis of projected images, which only allows to measure 2D features. In this paper, a method for the 3D morphological characterization of a compact aggregate from the analysis of a single image is proposed. This method is composed of three steps: the description of a stochastic geometric model, the acquisition of data from image analysis, and the fitting of the model parameters to the data using an optimization process. The method was validated using images of a calibrated 3D printed aggregate, and the results presented in the last section show discrepancies lower than 1% for 2D morphological characteristics and lower than 2% in most cases for 3D characteristics. The limitations of the model are discussed and suggestions for improvement are made in the conclusion.

**Index Terms**—Aggregates, Digital twins, Geometric modeling, Image analysis, Modeling, Simulation, Stochastic geometry

## I. INTRODUCTION

The morphological characterization of particle aggregates by image analysis is a common problem in many scientific fields such as the chemical industry [1, 2], the medical field [3, 4], the food industry [5–9] or civil engineering [10]. Depending on the characteristics studied and the type of aggregate, different techniques can be used: SEM [11], X-Ray CT images [10], video capture [12], multiple cameras [13] or multiple point of view [14]. More generally, the morphological characterization of an object such as an aggregate can have a different meaning depending on the context. Indeed, several types of morphological characteristics can be distinguished,

such as the characteristics of shape, size or texture [15] and, therefore, the physical characteristics such as the mass and chemical characteristics are generally excluded.

The most commonly calculated size characteristic is the Particle Size Density (PSD), which corresponds to the size density of each of the aggregates, and, when possible, the primary particle density, which corresponds to the size density of each of the primary particles of the aggregates. To this end, recent machine learning techniques allowing the segmentation of aggregates of particles of varying sizes have been successfully developed [16–19]. Regarding the shape characteristics, such as the elongation, the fractality or the porosity, these are particularly used to describe crystalline [3–5, 14] aggregates or coarse aggregates [10].

When it comes to characterizing aggregates by image analysis, two main categories of techniques exist. Direct methods propose to perform measurements directly on the images, using advanced image processing techniques [1, 20]. These methods are particularly effective when the images are of good quality, i.e. the shapes are easy to binarize and to isolate from each other. On the other hand, they become complex to implement when the number of objects to characterize is important or when they overlap. In this case, the use of indirect methods, such as stochastic methods based on models, can be very powerful [10, 11, 21–23]. The idea is then to model the aggregation phenomenon and to generate synthetic images with the same average characteristics as the real images. When there is a match, the characteristics of the real objects are known through the characteristics of the synthetic objects generated by the model.

## II. OVERVIEW & METHODOLOGY

The aim of this paper is to propose a method for the characterization of compact nanoparticle aggregates by image analysis and stochastic geometry. The problem at hand is the morphological characterization of a latex nanoparticle aggregate. This aggregate is the constituent of a powder whose grain size and shape has a considerable influence on the efficiency of the industrial processes in which it is used. The main goal is then the 3D morphological characterization of an aggregate of particles from a single 2D image. The 3D characterization of an aggregate from several images is a problem that has already been studied [6, 10], but the 3D characterization of an object from even multiple 2D measurements remains difficult [24]. Therefore, the proposed method is original because it allows to fully describe the 2D and 3D morphology of a particle aggregate when only one image is available by combining direct image analysis techniques with the use of a stochastic geometrical model.

The proposed method consists of three steps.

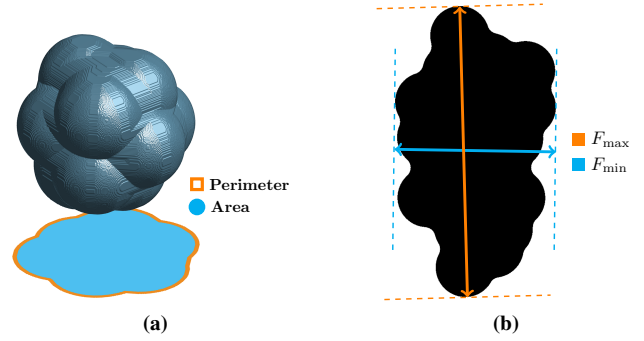
- 1) BLOSSOM<sup>1</sup>, a geometric stochastic parametric model for generating synthetic 3D aggregates of spherical particles of same size, is defined.
- 2) An aggregate image is analyzed and 2D morphological characteristics are measured. Image analysis is also used to calibrate certain parameters of the BLOSSOM model.
- 3) A cost function is defined and its optimization allows to determine an optimal set of parameters for the BLOSSOM model. With this optimal set of parameters, the synthetic aggregates have the same 2D morphological characteristics as those measured on the original image. This leads to the conclusion that the 3D morphological characteristics are also identical.

In the following section, the 2D and 3D morphological characteristics that will be measured and used throughout this paper are defined. The BLOSSOM model is then defined, and example implementations with different sets of parameters are presented. The fitting of the model to real data using image analysis is then described. In particular, a 3D printed aggregate of quasi-spherical particles is used to validate the method. Images of this aggregate were taken with a morphogranulometer (Morphologi G3 – Malvern Panalytical) and the 3D morphological characteristics of the 3D printed aggregate are known thanks to a reference STL file. It is worth mentioning that the 3D printed aggregate strongly resembles the latex nanoparticle aggregates mentioned in the previous section. The results of the optimization are presented and explained in the last section. In particular, the 3D characteristics predicted by the BLOSSOM model are compared to those contained in the STL file. Finally, the limitations of the model are discussed and possible improvements are suggested.

## III. MORPHOLOGICAL CHARACTERIZATION

In this section, the 2D and 3D morphological properties that will be used to characterize particle aggregates are defined.

<sup>1</sup>BLOSSoming Overlapping Spheres Self-Organizing Model



**Fig. 1:** (a) Illustration of the projected area (blue) and perimeter (red) of an aggregate. (b) Illustration of the calculation of the maximum and minimum Feret diameters.

a) *Aspect ratio:* The aspect ratio  $\Psi_{AR}$  is defined as the ratio of the minimum and maximum Feret diameters.

$$\Psi_{AR} = F_{\min}/F_{\max} \in [0; 1]. \quad (1)$$

b) *Projected area and perimeter:* The projected area and perimeter are usually measured on binary images of an aggregate projection along an axis. Depending on the 3D morphology of the aggregate and the axis considered, these characteristics can change significantly (Fig. 1a).

c) *Feret diameters:* The Feret diameters of a binary shape correspond to the distance between two parallel lines arranged in such a way that the shape is located exactly between these two lines. The maximum (resp. minimum) Feret diameter corresponds to the maximum (resp. minimum) possible distance between these two lines (Fig. 1b).

d) *Centroid:* The centroid of a binary shape is the point corresponding to the center of mass of the pixels (or voxels in 3D) belonging to the shape.

e) *Volume:* The volume of an aggregate  $V$  is usually calculated by summing a number of voxels of a 3D binary shape in a discrete space.

f) *Convex volume:* The convex volume  $V_c$  is the volume of the convex envelope of a 3D shape.

g) *Solidity and porosity:* The solidity  $SLD \in [0; 1]$  is the ratio of the volume  $V$  over the convex volume  $V_c$ .

$$SLD = V/V_c. \quad (2)$$

Low strength may indicate high porosity  $\phi$  of the aggregate, the latter being defined as follows.

$$\phi = V_{\text{pores}}/V. \quad (3)$$

h) *Surface area:* The surface area  $S$  is the closed surface of a 3D shape.

i) *Equivalent diameter:* The equivalent diameter or equivalent spherical diameter (ESD) is the diameter of a sphere having the same volume as the considered 3D shape.

$$ESD = \sqrt[3]{\frac{6 \times V}{\pi}} \quad (4)$$

j) *Principal axis length*: The principal axis length (PAL) correspond to the length of the three major axes of the ellipsoid having the same co-variance matrix as the voxels representing the considered 3D binary shape.

#### IV. STOCHASTIC MODEL

##### A. Model definition

The generation of an aggregate by the BLOSSOM model corresponds to an iterative process. At each iteration, a hard sphere is added to the aggregate being generated. A parameter  $d_\alpha$  allows a certain overlap distance between the spheres. This process can be described as follows.

- 1) A spherical particle is created at coordinates  $(0; 0; 0)$ . During the whole process, if the particle is not in contact with another particle (according to  $d_\alpha$ , the overlap parameter), it stands still and the next iteration is performed.
- 2) A direction vector  $\vec{v} = (\Delta\rho, \theta, \varphi)$  is drawn at random, and the particle will then move along this direction, the displacement step depending on the parameter  $\Delta\rho$ . The probability density functions related to  $\varphi$  and  $\theta$  are respectively  $f_\varphi$  and  $f_\theta$ .
- 3) When the current particle stops moving, and if the maximum number of particles  $N_p$  has been reached, the process stops. Otherwise, a new particle is created, and the process goes to the next iteration.

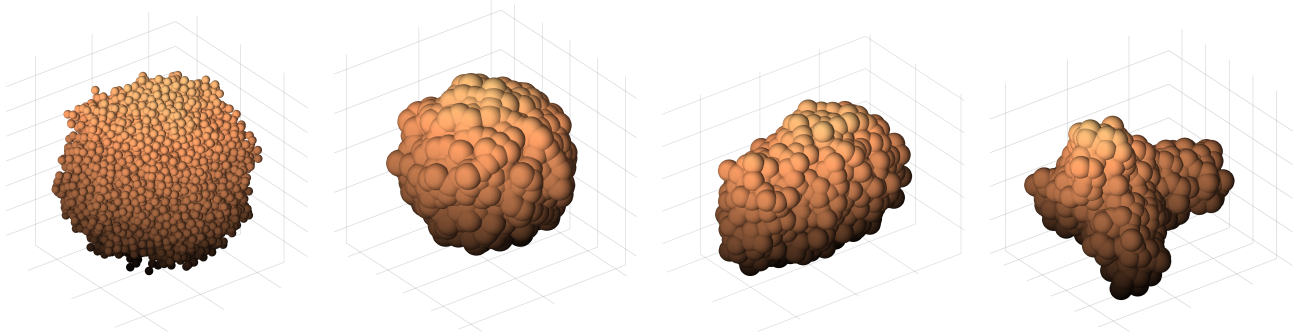
The BLOSSOM model depends on 4 numerical parameters (Tab. I) and 2 probability density functions to express the

random coordinates of the vector  $\vec{v}$  determining the direction of the moving particle at each iteration. These coordinates are expressed in spherical coordinates. Regarding the overlap parameter  $d_\alpha$ , it is expressed as a ratio of the diameter of the particles. Thus,  $d_\alpha = 0$  indicates that only single point contacts are allowed, while a ratio of  $d_\alpha = 0.5$  authorizes an overlap of 50% of the diameter, i.e. of the radius  $r$  of the particles.

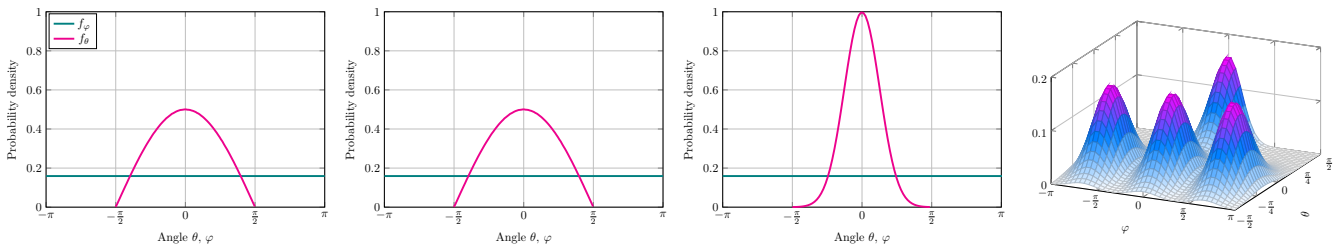
**TABLE I:** Listing of the BLOSSOM model parameters.

Parameters	Definition
$N_p$	Number of particles
$r$	Radius of the particles
$d_\alpha$	Overlap parameter
$\Delta\rho$	Displacement step
$f_\theta, f_\varphi$	Probability density functions

In order to ensure that each particle has at least one point of contact with the aggregate being generated, a reassembly operation is performed at the end of each iteration. In addition, a repulsive force of low intensity relative to the displacement step is added to the aggregate being generated, so that the mobile particle finds an available location more quickly. This also prevents the aggregates from being too porous in the case of a high displacement step. More precisely, in case of an overlap greater than  $d_\alpha$ , the mobile particle is repelled according to a vector  $\vec{u}$  in a direction orthogonal to the vector  $\vec{v}$ , and whose modulus is a fraction of  $\Delta\rho$ , proportional to the overlap.



**Fig. 2:** Examples of aggregates generated by the BLOSSOM model with, from left to right, a number of particles  $N_p = \{5000, 1500, 1000, 1000\}$ , an overlap parameter  $d_\alpha = \{0, 0.75, 0.5, 0.6\}$ , and density probability functions  $f_\theta$  and  $f_\varphi$  displayed on Fig. 3. The parameters  $r$  and  $\Delta\rho$  are constant.



**Fig. 3:** Probability density functions used to generate the aggregates in Figure 2. The probability densities allow a uniform distribution on the sphere for the first two aggregates, and  $f_\theta$  is a von Mises distribution [25] for the third aggregate while  $f_\varphi$  and  $f_\theta$  are a joint mixture of four normal distributions for the fourth one.

### B. Example of realizations

Figure 2 shows some examples of realizations of the BLOSSOM model using different sets of parameters. The overlap parameter  $d_\alpha$  has a direct impact on many morphological characteristics of the aggregates, such as porosity  $\phi$ , solidity SLD or surface area  $S$ . The probability density functions  $f_\theta$  and  $f_\varphi$  (Fig. 3), and, not surprisingly, the number of particles  $N_p$ , have an significant impact on the shape and size of the aggregate.

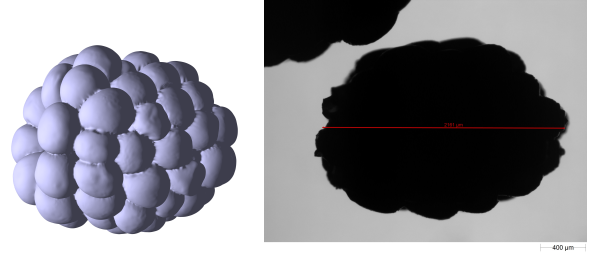
In particular, if  $f_\theta$  and  $f_\varphi$  are constant, the aggregates are rather spherical and as long as  $f_\varphi$  remains constant, the aggregates have some cylindrical symmetry. Joint distributions for  $f_\theta$  and  $f_\varphi$  allow to generate more complex aggregates with concavity and lower solidity SLD. Finally, a large overlap parameter  $d_\alpha$  allows to generate aggregates with high porosity  $\phi$ .

### C. Performance

In terms of performance, the BLOSSOM model being coded in MATLAB®, the generation of the 192 aggregates with  $N_p = 200$  takes about 5 seconds on a machine equipped with an Intel® Core™ i9-12900KF processor at 3.19Ghz and 64GB of RAM. The generation of an aggregate of 5000 particles is of the order of a tenth of a second on the same machine. The parameters with the most influence on the performance of the model are the number of particles  $N_p$  and the displacement step  $\Delta\rho$ . Indeed, the larger  $\Delta\rho$  is, the faster the aggregate will blossom.

## V. MODEL FITTING AND VALIDATION

In this section, the method for fitting the BLOSSOM model parameters to real data is presented. For this purpose, an aggregate of quasi-spherical particles was 3D printed. The 3D morphological characteristics of this aggregate are well known, as they are contained in a reference STL file (Fig. 4). Then, 2D projection images of the aggregate were made using a morphogranulometer and then binarized (Fig. 4 & Fig. 5a). In order to adjust the model parameters to the actual data, an optimization process must be applied to a cost function. The cost function, defined later by equation (7), will allow to compare the 2D morphological characteristics of the synthetic aggregates generated by the BLOSSOM model to



**Fig. 4:** Left: Visualization of the reference STL file containing the 3D structure of the aggregate to be 3D printed. Right: Raw image from the morphogranulometer.

those of the 3D printed aggregate. To do this, the images from the morphogranulometer are used, and the necessary measurements are performed.

Nevertheless, in order to work properly, the model requires two probability density functions. The following section presents a method to estimate  $f_\theta$  by image analysis and makes a hypothesis about  $f_\varphi$ .

### A. Computing $f_\theta$ and $f_\varphi$ with image analysis

In a spherical coordinates system, a point in space is defined by three numbers:

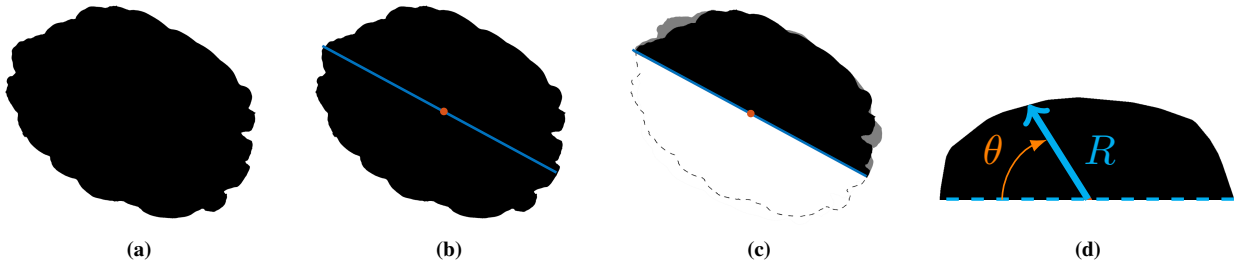
$$\rho \in \mathbb{R}_+, \quad \varphi \in [-\pi; \pi] \quad \text{and} \quad \theta \in [-\pi/2; \pi/2]. \quad (5)$$

In order to simplify the problem, it is assumed that the aggregates to be characterized offer a certain cylindrical symmetry, as in the third example in Fig. 2. This immediately translates into the fact that the probability density function of  $\varphi$  is uniform, i.e.

$$\varphi \sim \mathbb{U}(-\pi, \pi) \quad (6)$$

where  $\mathbb{U}$  is the continuous uniform distribution.

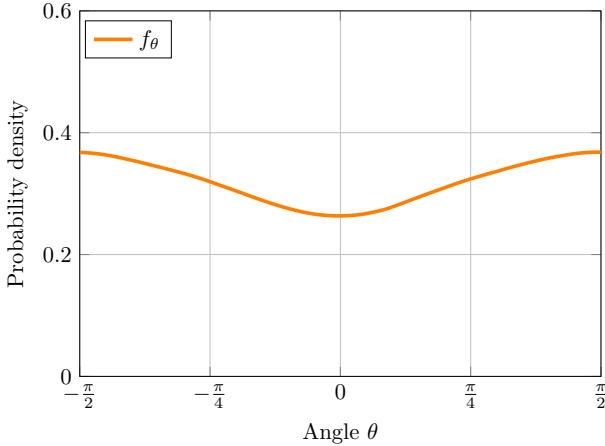
For the characterization of  $f_\theta$ , a binary image of the aggregate to be characterized is used. The centroid of the shape is calculated (Fig. 5b) and the shape is split in two along a line parallel to the maximum Feret diameter passing through the centroid. A symmetry operation is performed on one of the two sub-images, and after the two parts are merged together



**Fig. 5:** From left to right: Image from the morphogranulometer after binarization (5a), calculation of the centroid of the shape and alignment of the line in the direction of  $F_{\max}$  (5b), merging of the two opposite halves (5c) and calculation of the probability density function  $f_\theta$  (5d).

(Fig. 5c), the convex hull of the resulting shape is computed. For each angle  $\theta \in [-\pi/2; \pi/2]$ , the maximum length  $R$  between the centroid computed earlier and the shape boundary is calculated (Fig. 5d). Fig. 5 illustrates these different steps.

After computing the maximum distance  $R$  for several values of  $\theta$ , an estimate of the probability density  $f_\theta$  is calculated, as shown in Fig. 6.



**Fig. 6:** Probability density function  $f_\theta$  estimated from the aggregate projection image from the morphogranulometer in Fig. 5.

### B. Cost function definition

Once the two probability density functions  $f_\theta$  and  $f_\varphi$  are computed, the other 4 parameters of the model must be fitted to the real data. In order to do so, a cost function must be defined. The general idea is to generate multiple synthetic aggregates and compare their 2D morphological characteristics to those measured on the aggregate images from

the morphogranulometer. Therefore, the cost function allows to quantify the differences between the measured morphological characteristics and is defined as follows.

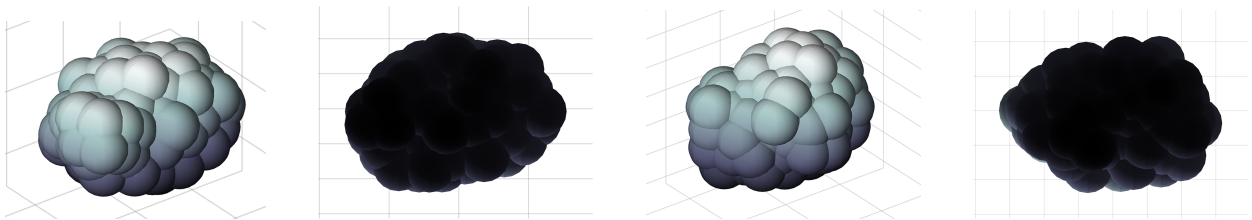
$$F_{\text{cost}}(\omega) = 3\Delta(A_p) + 3\Delta(P) + 3\Delta(\Psi_{AR}) + \Delta(F_{\text{max}}) + \Delta(F_{\text{min}}) \quad (7)$$

with  $A_p$  the projected area,  $P$  the perimeter,  $\Psi_{AR}$  the aspect ratio,  $F_{\text{max}}$  (resp.  $F_{\text{min}}$ ) the maximum (resp. minimum) Feret diameter and  $\omega = \{N_p, r, d_\alpha, \Delta\rho\}$  a set of 4 parameters of the model. The quantities  $\Delta x$  represent the relative errors between a characteristic  $x$  measured on an aggregate generated by the model with the set of parameters  $\omega$  and the result of the measurement performed on an image from the morphogranulometer. Regarding the weights associated with each of the relative errors, they were determined empirically. In particular, the errors on the Feret diameters were added in order to better fit the distance step parameter  $\Delta\rho$ .

### C. Model validation

The validation of the model consists in finding an optimal set of parameters  $\tilde{\omega}$  by minimizing the cost function  $F_{\text{cost}}$  and then comparing the 3D morphological characteristics of the aggregates generated by the BLOSSOM model with  $\tilde{\omega}$  (Fig. 7) to those of the 3D printed aggregate, whose 3D morphological characteristics are known thanks to the STL file. The optimization is performed using a simulated annealing algorithm. At each iteration, 192 aggregates are generated from the same set of parameters and the morphological characteristics measured are being averaged before being compared to those of the real images.

The results of the optimization process are presented in Table II. It is noticeable that all the characteristics measured on the synthetic aggregates are extremely close to those of the reference aggregate, with the single exception of the surface area  $S$ . Indeed, the relative errors on the 2D characteristics are



**Fig. 7:** Examples of aggregates generated by the BLOSSOM model using the optimal set of parameters  $\tilde{\omega}$  with their respective projections. The direction of projection is always determined by the vector  $\vec{n} = (1, 0, 0)$ , whether in Cartesian or spherical coordinates, in order to remain consistent with the way the distribution  $f_\theta$  was estimated.

**TABLE II:** Comparison of 2D and 3D morphological properties measured on the 3D printed reference aggregate and those proposed by the BLOSSOM model from the optimal set of parameters  $\tilde{\omega}$ , averaged over 192 realizations.

Properties	2D			3D							
	$A_p$ (mm <sup>2</sup> )	$P$ (mm)	$\Psi_{AR}$	$V$ (mm <sup>3</sup> )	$V_c$ (mm <sup>3</sup> )	$S$ (mm <sup>2</sup> )	SLD	ESD (mm)	PAL <sub>1</sub> (mm)	PAL <sub>2</sub> (mm)	PAL <sub>3</sub> (mm)
Ground truth	2.73	6.75	0.71	2.34	2.76	11.25	0.84	1.65	1.98	1.54	1.52
BLOSSOM model	2.73	6.73	0.71	2.32	2.75	10.19	0.84	1.65	2.06	1.56	1.55
Error (%)	0.1%	0.2%	0.3%	0.6%	0.1%	9.4%	0.3%	0.2%	4.1%	1.6%	2.2%

less than 1%, and the errors on the 3D characteristics are also less than 2% in most cases. The specific case of the higher relative error on the surface area  $S$  can probably be partly explained by the fact that the 3D structure contained in the STL file is not convex and presents a strong concavity at one of the tips of the aggregate. This leads to an increase in the surface area of the reference aggregate, which remains difficult to quantify, without being apparent on the 2D projections from the morphogranulometer.

Another reason, more subtle, can be related to the errors made on the PAL. Indeed, one can see that PAL<sub>2</sub> and PAL<sub>3</sub> are not identical, which partially invalidates the initial hypothesis of a cylindrical symmetry of the aggregate. Therefore, relatively larger errors are made on PAL<sub>2</sub> and PAL<sub>3</sub> and, since the surface area  $S$  of a flattened cylinder is larger than the one of a perfect cylinder, it seems natural that this characteristic is again slightly underestimated.

#### D. Comparison with other methods

Comparing the performance of the proposed method with others is difficult. Indeed, a first reason is the fact that the estimation of the 3D morphological characteristics of an aggregate is usually done from several images, with multiple cameras [13] or a mobile one [14] whereas our approach uses only one single image.

Moreover, one of the main reasons why the comparison is difficult is that the ground truth is usually unknown. Under these conditions, it is impossible to estimate the error on the measured characteristics. The proposed approach allows this only because a calibrated 3D printed aggregate is available.

Nevertheless, [14] propose an estimation of the relative error using a method based on a 3D reconstruction from a mobile camera for crystalline aggregates. The relative errors are estimated for a sphere, a cylinder and an hexagonal prism and are in the range of 1% to 3.5%, both for the volume  $V$  and the surface area  $S$ .

Hence, even an approach based on multiple images of rather simple objects does not provide a better estimate of the volume  $V$  than the BLOSSOM model does. As for the surface area  $S$ , the relative error made by the method proposed in this paper remains higher, but it is to be put in perspective with the shape of the aggregate studied, which is far more complex, and the nature of the aggregate, which is not a crystal, but made of spherical primary particles.

## VI. CONCLUSION

The results presented in the previous section show that it is possible to validate the proposed method on a specific case, with very good results on all the measured morphological characteristics (2D and 3D), except for the surface area, although some explanations have been proposed to explain this discrepancy. In particular, the BLOSSOM model was shown to be flexible enough to be able to generate spherical particle aggregates with the same morphological characteristics as the 3D printed aggregate from a reference STL file.

That being said, there are still many areas for improvement. Indeed, the error on the surface area can probably be reduced by giving up the assumption of a cylindrical symmetry. Nevertheless, this strong assumption is mainly due to the fact that only a single 2D projection is used, which tremendously reduces the knowledge of the aggregate to be characterized. Indeed, the use of multiple uncalibrated projections is under study and will be the focus of future work.

Moreover, one of the next steps is the application of the method to the characterization of real aggregates, with images acquired directly in-situ in the industrial reactor. The enhancement of the model, through the use of non-spherical particles or of different size is also an interesting idea, especially since the particles used to print the 3D aggregate are themselves neither perfectly spherical, nor of identical size.

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