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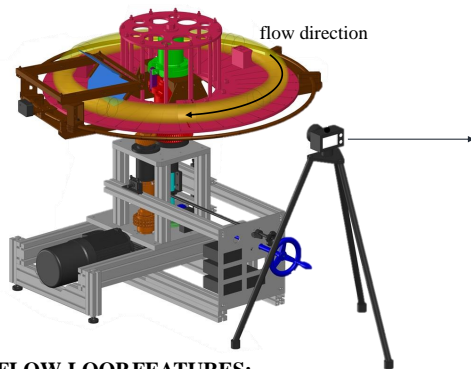
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Graphical Abstract

Gas-liquid flow regimes in a novel rocking and rolling flow loop

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ROCKING AND ROLLING RING FLOW LOOP New Benchtop Apparatus for Two-phase Flow Dynamics Studies



FLOW-LOOP FEATURES:

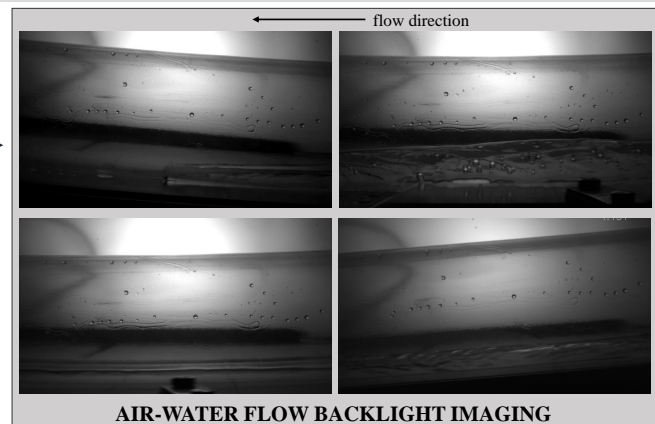
LxWxH = 1.2 x 1.2 x 1.2 m³

Diameter of the tube: 69.85 mm

Volume of the loop: ~ 10 L

Flow induction: mechanical without pumping

Control parameters: liquid loading, rocking angle and rate.



AIR-WATER FLOW BACKLIGHT IMAGING

- Flow regimes determination and mapping
- Liquid height measurements (model validation parameter)

Highlights

Gas-liquid flow regimes in a novel rocking and rolling flow loop

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- A novel flow-testing benchtop without pumping is designed.
- Backlight imaging is adopted to characterize flow behaviour.
- The influence of centrifugal force on flow regimes and flow transitions are analysed.
- Energy minimization, mechanistic and combined models are applied to predict the flow.

Gas-liquid flow regimes in a novel rocking and rolling flow loop

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Abstract

Predicting two-phase flow pattern characteristics and flow transition is fundamental to address several industrial problems, *e.g.* for the oil and gas industry. In order to fulfill the upscaling from the laboratory to the industrial scale, resource-efficient flow testing facilities which closely replicate industrial flow characteristics are needed. To address this, we introduce a new experimental device named as the Rocking and Rolling Ring Flow Loop (3RFL), which is size, cost, and time-efficient. In the present work, we employ the 3RFL apparatus at atmospheric pressure and temperature, with air and water as working fluids. However, the ultimate goal of our work is to build an experimental set-up capable of capturing the under-pressure reactive multiphase flow (gas-liquid-solid) dynamics typical of flow assurance in oil production and transportation. At the moment, the 3RFL can induce different flow regimes by adjusting the system control parameters such as rocking angle, rocking rate, and liquid volume fraction, all without requiring a pump. We observe three flow regimes, and analyze the impact of control parameters on their emergence. Our findings reveal that flow regime transitions are influenced by the competition between gravitational and centrifugal forces, which arise due to the curvature of the tube. Among three employed modeling strategies, namely mechanistic modeling, total energy minimization and a combined approach, we find that the total energy minimization model best compares to the experimental liquid height.

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Keywords: Ring flow loop, Gas-liquid flow, Flow regime prediction, Backlight imaging, Energy minimization model

1. Introduction

Gas-liquid flow transport is a common occurrence in various industrial processes, and it becomes particularly challenging in oil and gas flowlines. The extraction of oil can lead to the formation of gas hydrates, which are ice-like crystals resulting from the entrapment of light hydrocarbon molecules in the water lattice structure (Sum et al., 2009; Balakin, 2010). These gas hydrates pose significant financial and safety risks since they are adhesive and, therefore tend to agglomerate and stick to the pipe wall, and finally block the flow (Kinnari et al., 2008; De Almeida et al., 2023). Traditional solutions for this problem are based on the avoidance of hydrate formation, which is achieved by injection of environmentally harmful chemical additives in large quantities. Today, the acceptance strategy proposes the use of anti-agglomerants to mitigate particle adhesion and thereby enable flow transportation along with hydrates (Kinnari et al., 2015). However, this strategy is based on the co-existence of gas/liquid phases along with the solid phase, for which a strong interplay is expected. Melchuna (2016) reported that the gas-liquid flow influences the kinetics of hydrate growth and, consequently, the crystal size and location. De Almeida et al. (2023) showed that the water-cut, *i.e.* the volume of water in oil, strongly influences the hydrate onset formation and the plugging risk. Conversely, hydrates intrinsically consume water, therefore flow characteristics change. For instance, at 50% water-cut, hydrate formation might lead to a change in the continuous carrying phase (from oil in water to water in oil). As such, successful implementation of hydrate management strategies requires a deep knowledge of two-way coupling between hydrate formation and multiphase flow characteristics, *e.g.* pressure drop, liquid holdup and flow regime.

Nowadays, there is a wide range of experimental apparatus dedicated to studying hydrate crystallization and transport. The key criteria that apparatus must meet when studying flow-dependent phenomena of hydrate formation are the ability to reproduce flow regimes and to control flow variables, providing interpretative experimental data along with flow visualization. Although pilot-scale flow loops meet most of these requirements, they have drawbacks such as high investment, reduced cooling capacity and large required time to conduct test campaigns. To facilitate time and cost-efficient

35 laboratory testing coupled with modelling procedures, benchtop testing sys-
36 tems are needed. Examples of benchtop apparatus are Rock Flow Cell (RFC)
37 (Sa et al., 2019) and Euler Wheel (Kelland et al., 2015). The RFC is made
38 up of an o-ring-sealed straight pipe (less than 1 meter long) with a diameter
39 of a few centimeters mounted on a horizontal mobile table which tilts back
40 and forth by an electric motor at a controlled rate and angle. Thus, unlike
41 in pilot-scale flow loops, the gravitational force acting downward drives fluid
42 flow, eliminating the influence of the pump on particle flow. Flow visualiza-
43 tion in the RFC system is afforded by two windows located at both ends of
44 the pipe. By varying the liquid loading, rocking angle and rate, the RFC can
45 readily replicate various flow regimes, such as stratified, stratified-wavy, slug,
46 and dispersed bubble. This allows one to comprehend the flow-dependent
47 phenomena of hydrate formation. Other benefits of the RFC are low capital
48 and operational expenses, short test times and repeatability of the results.
49 Moreover, the compactness of the RFC opens up the possibility of applying
50 computational fluid dynamics (CFD). However, the flow in the RFC often
51 changes direction due to collisions with the ends of the tubes, which leads to
52 a disturbance of the flow.

53 The Euler wheel consists of a narrow pipe (whose diameter is smaller
54 than 30 mm) coiled to form a wheel mounted on a horizontal disc. Flow
55 circulation is initiated by the rotation of a spherical ball along the wheel.
56 Such kinematics permits reproducing pipeline flow. The maximum velocity
57 of the fluid reaches 1.2 m/s (Kelland et al., 2015). The onset of hydrate
58 formation can be detected by monitoring the pressure of the system and by
59 visual observations. Same as for the RFC, the Euler wheel allows time and
60 cost-efficient testing without a pump. However, the reproduction of flow
61 regimes, such as those observed in flow lines, is hard to achieve as the ratio
62 of the tube length to the diameter is small (~ 10).

63 To eliminate these shortcomings, we present a new experimental appa-
64 ratus that can generate flow velocities approaching those of the industrial
65 fields and different pipeline flow regimes. This apparatus is dubbed Rocking
66 and Rolling Ring Flow Loop (3RFL) and has been designed and assembled
67 at Mines Saint-Etienne. It consists of a transparent cellulose acetyl butyrate
68 ring loop ($d = 69.85$ mm, $D = 840$ mm) installed on a horizontal mobile
69 platform. This platform rolls sequentially by four sides, *i.e.* to the right,
70 front, left, and back, driven by an electrical motor. Compared to the RFC,
71 in the 3RFL additional "rolling" motion over the y-axis is added (Fig. 1).
72 This resulted in a smoother flow resembling a flowline. The transparency of

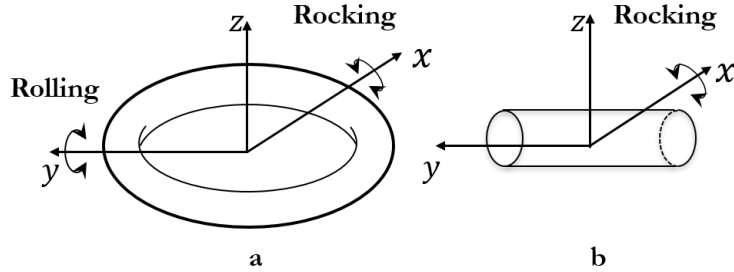


Figure 1: Sketch of the kinematics of the rocking-based types of experimental apparatus: (a) rocking and rolling ring flow loop (this work) and (b) Rock Flow Cell (Sa et al., 2019).

73 the loop allowed us to apply backlight imaging tomography to characterize
 74 the flow.

75 The ultimate aim of our work is to build an experimental set-up capable
 76 of capturing the reactive multiphase flow (gas-liquid-solid) dynamics
 77 typical of flow assurance issues. In particular, we are interested in the hy-
 78 drate formation and in the interplay between crystallization and fluid flow.
 79 Methane hydrates form under particular conditions of pressure and temper-
 80 ature ($P > 80$ bar and $T < 4^\circ$). In the last 30 years, several studies have
 81 been done in the SPIN centre at Mines Saint-Etienne to experimentally char-
 82 acterize, in batch reactors and pipe reactors, the hydrate formation for flow
 83 assurance. The main outcome is the Archimede flow loop (Fidel-Dufour et al.,
 84 2005; Melchuna, 2016; Herri et al., 2017; Pham et al., 2020; De Almeida et al.,
 85 2023): a multi-instrumental 50-meter long flow loop capturing the hydrate
 86 formation under water-oil-gas flow. However, in the Archimede flow loop,
 87 the gas phase is solely dissolved into the liquid, resulting in the impossibility
 88 to observe typical flow patterns of flow assurance, such as gas-liquid strati-
 89 fied, slug flow or annular flow. Also, visualisation of the flow is only possible
 90 via a small (a few centimeter long) window. These issues have prompted
 91 us to build the 3RFL apparatus with the aim to have a small-scale set-up
 92 with transparent tubes allowing us to observe a larger range of flow patterns.
 93 However, the step-by-step development strategy of the 3RFL system is simi-
 94 lar to what we have pursued for the Archimede flow loop. Firstly, the loop is
 95 employed at ambient pressure and temperature, with air and water as work-
 96 ing fluids. This is the study introduced in the present work. Secondly, the
 97 loop will be operated at conditions closer to those of the oil production and
 98 transport (oil-water-methane flows under high pressure and low temperature)

99 and equipped with more advanced experimental techniques qualified to work
100 under high pressures and low temperatures. This study will be addressed in
101 future works.

102 Nonetheless, the 3RFL has certain constraints, including the complexity
103 of handling very high liquid volume fractions, as the system strongly relies on
104 liquid motion, and dry-out which is challenging to model. Also, reproducing
105 annular flow within the 3RFL is not possible. Indeed, annular flow occurs
106 when the gas velocity is significantly higher than the liquid velocity, as the
107 gas flow generates liquid atomization leading to the formation of droplet
108 touching the upper wall and forming a liquid film. In our system the gas
109 phase is simply driven by the shear exerted by the liquid flow, limiting the
110 gas velocity to relative low values. In addition, flow in curved tubes is more
111 complex in nature than flow in straight tubes. As reported by Eustice (1911)
112 and Dean (1927), who studied single-phase flow, the complexity lies in the
113 effect of tube curvature-induced centrifugal force which develops a secondary
114 flow leading to active radial mixing. It is possible to imagine that adding a
115 supplementary phase, such as oil, would add yet another layer of complexity
116 to the flow behaviour.

117 Given the difficulties and the challenges that we might face in fully char-
118 acterizing - by means of experiments - such a complex multiphase flow, we
119 complement the experimental work presented herein with modeling develop-
120 ment, which in turns is helpful to study the effect of varying fluid properties
121 and flow conditions, *e.g.* replacing water with oil. In particular, we employ
122 three different modeling approaches: mechanistic model, total energy min-
123 imization model and a hybrid model built by combining the previous two
124 strategies. As for the 3RFL system, also in the modeling development we
125 adopt a step-by-step strategy. Firstly, we consider a simple 1D model ne-
126 glecting curvature effects, de-wetting and wavy gas-liquid interface. This is
127 introduced in the present study. In future works, the model will be upgraded
128 to take into account those effects, in addition to a third phase (oil), pressure
129 and temperature effects and hydrate kinetics of crystallization.

130 Both the mechanistic and the total energy minimization approaches are
131 usually employed to characterize gas-liquid flows in pipelines. Analytical
132 models have been developed since the early work of Taitel and Dukler (1976a).
133 The authors established a mechanistic model to predict five basic flow pat-
134 terns, such as stratified smooth, stratified wavy, annular, intermittent and
135 dispersed bubbles. More importantly, their model takes into consideration
136 many factors that affect flow configuration, including geometrical parame-

137 ters, *e.g.* pipe diameter and inclination angle, physical parameters, *e.g.* den-
138 sity and viscosity of phases and operational parameters, *e.g.* two-phase flow
139 rates. However, mechanistic models employ closure relationships for wall and
140 interfacial shear stresses. Following Taitel and Dukler (1976a), many differ-
141 ent friction factor expressions have been established to describe the closure
142 relations at the interface (Amaravadi, 1994; Ouyang and Aziz, 1996; Xiao
143 et al., 1990; Garcia et al., 2003). However, they remain to be empirical and
144 different from one study to another. An important limitation of mechanistic
145 models is that multiple solutions might exist in terms of equilibrium liquid
146 height h_L for the same flow configurations. This was highlighted by several
147 studies (Landman, 1991; Taitel and Barnea, 1990; Barnea and Taitel, 1992,
148 1994; Ullmann et al., 2003; Thibault et al., 2015).

149 More recently, other modeling strategies have been developed to overcome
150 the problem of closure relations at the interface typical of mechanistic models.
151 Chakrabarti et al. (2005) have been the first to use the energy minimization
152 approach to estimate two-phase flow parameters such as liquid holdup and
153 pressure gradient for two-phase flow. It has been assumed that the system
154 would stabilize to its minimum energy, while the pressure gradient in both
155 phases would be the same. The steady state, stratified liquid-liquid hori-
156 zontal flow with a flat interface has been considered in their study. After
157 Chakrabarti et al. (2005), the total energy minimization approach found its
158 continuation in the work of Sharma et al. (2011). Sharma et al. (2011) ap-
159 plied the total energy minimization model to predict five flow patterns for
160 horizontal and near horizontal oil-water flows. Lee et al. (2013) have been
161 the first to employ the energy minimization concept to predict gas-liquid
162 stratified flow characteristics. The authors considered gas-liquid flow as a
163 dissipative process and that the structure of the gas-liquid flow must be the
164 one that minimizes the dissipated energy within a control volume of a pipe.
165 Assuming a flat interface between phases, continuity of pressure gradients in
166 both phases and constant velocity profiles, the authors suggested that the
167 minimum dissipated energy corresponds to the minimum pressure gradient.
168 The pressure gradient of the system has been expressed as a sum of gas
169 and liquid phases' momentum conservation equations, such that the final
170 equation is released from the interfacial shear stress component (Lee et al.,
171 2013).

172 To conclude, the aim of our work is to overcome the above-mentioned
173 shortcomings of compact apparatus, such as Rock Flow Cell and Euler wheel,
174 and pilot-scale apparatus, as the Archimede flow loop developed in the last

175 decades at Mines Saint-Etienne. For this, we introduce here a novel flow loop,
176 whose rocking and rolling motion promotes the occurrence of flow patterns
177 under typical hydrodynamic conditions of flow assurance problems. We leave
178 to future studies the improvements of such a flow loop to account for ther-
179 modynamics conditions fostering hydrate formation. Meanwhile, we compare
180 the experimentally observed liquid heights to the predictions of three differ-
181 ent modeling strategies, of which one is a novel hybrid approach developed
182 by combining mechanistic and total energy minimization modeling.

183 The article is structured as follows. Section 2 presents details on the flow
184 testing procedure, including an extensive description of the experimental
185 apparatus, flow visualization elements, system control parameters, and flow
186 testing procedure. Section 3 discusses the observed flow characteristics, such
187 as flow regimes, flow regime transitions, and liquid height, depending on the
188 control parameters of the flow. Further, section 4 describes three modeling
189 approaches applied for predicting the liquid height of the studied flow and
190 compares the obtained predictions against experimental results. Finally, in
191 section 5 key outcomes are summarized.

192 **2. Methodology**

193 *2.1. Description of experimental setup*

194 The Rocking and Rolling Ring Flow Loop (3RFL), illustrated in Fig. 2,
195 measures 1.2 meters in height, width, and length. The apparatus base is
196 constructed using aluminium blocks (in grey). The 3RFL consists of a trans-
197 parent ring loop (G in Fig. 2) installed on a horizontal mobile platform. As
198 the name of the apparatus suggests, the “rocking and rolling” characterizes
199 the nature of the mechanical motion of the platform while the “ring” iden-
200 tifies the flow testing loop geometry. The platform itself is a circular acrylic
201 disc with a diameter of $D = 0.96$ m, featuring a circular cut-out in the
202 centre. This platform is attached to a metal hood (E in Fig. 2), which in
203 turn is mounted on the slave rotor (B in Fig. 2). The platform, driven by
204 mechanical motion, tilts sequentially by four sides, *i.e.* to the right, front,
205 left, and back. In this way, controlled flow within the loop is induced. To
206 have a better idea of how this device works, please refer to Video 1 in the
207 supplementary materials. Two parameters drive the ring loop: the rocking
208 angle (θ) measured in degrees and the rocking rate (f_R) measured in oscilla-
209 tions per minute (*opm*). Note that one oscillation per minute of the ring loop
210 corresponds to one revolution per minute (rpm) of the rotating central shaft,

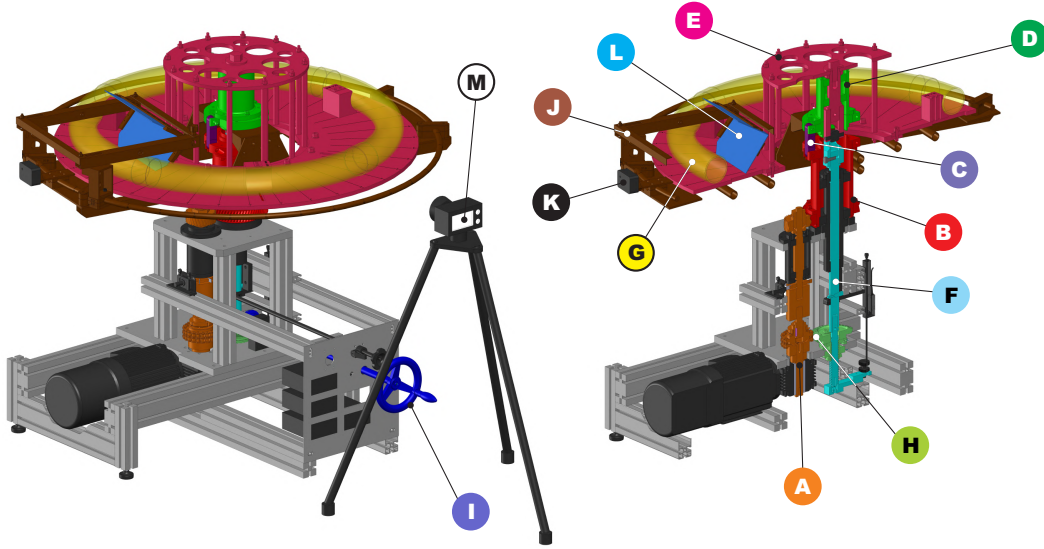


Figure 2: Sketch of the Rock&Roll Ring Flow Loop (3RFL) and main elements. A: Driveshaft / B: Rotor / C: Connecting rod / D: Slave rotor / E: Metal disc / F: Central shaft / G: Torus tube / H: Turning nut / I: Hand wheel shaft / J: Rotary arm (and linked parts) / K: Action camera / L: Mirrors / M: High-speed camera.

211 to be introduced later. Other control parameters of the system are the liquid
 212 volume fraction and the ring loop dimensions, *e.g.* diameters of the tube (d)
 213 and of the ring (D). In Table 1 limits of variation of control parameters and
 214 the possibility of their modification while operating are given.

215 The apparatus is equipped with a temperature probe, displacement (to
 216 adjust θ), and inductive sensors (to adjust f_R). To facilitate air-water flow
 217 observations, two different cameras were used - specifically, action and high-
 218 speed cameras (labelled as K and M respectively in Fig. 2). The action
 219 camera was employed along with a mirror system (L in Fig. 2). There are two
 220 types of mirror systems, one is entitled to project the top view, and another
 221 is the back view of the flow. The system of mirrors and the action camera
 222 are mounted on the rotary arm (J in Fig. 2) and therefore rotate about the
 223 central axis of the 3RFL following the flow. The action camera (GoPro Black
 224 Hero 9) and mirrors are arranged in such a way that the video captures both a
 225 side view of the tube and a top (or back) view, which is projected through the
 226 mirror (see Video 5 in supplementary materials). Meanwhile, the high-speed
 227 monochromatic camera was combined with backlighting. The high-speed

Control Parameters	Notation	Unit	Range	Adjustable during the test
Rocking rate	f_R	opm	3-36.2	Yes
Inclination angle	θ	$^\circ$	0-45	Yes
Diameter of the ring	D	mm	500-900	No
Diameter of the tube	d	mm	6 - 80	No
Liquid volume fraction	φ_L	—	0-1	No

Table 1: Control parameters of the 3RFL apparatus and their range of variations as well as the potential for their change during the test.

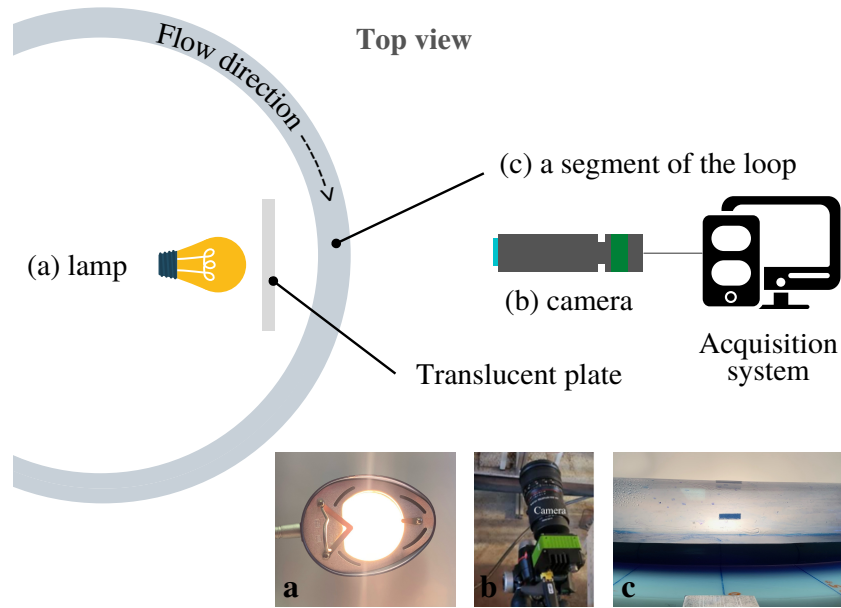


Figure 3: A sketch of air-water flow backlighting imaging with a high-speed camera.

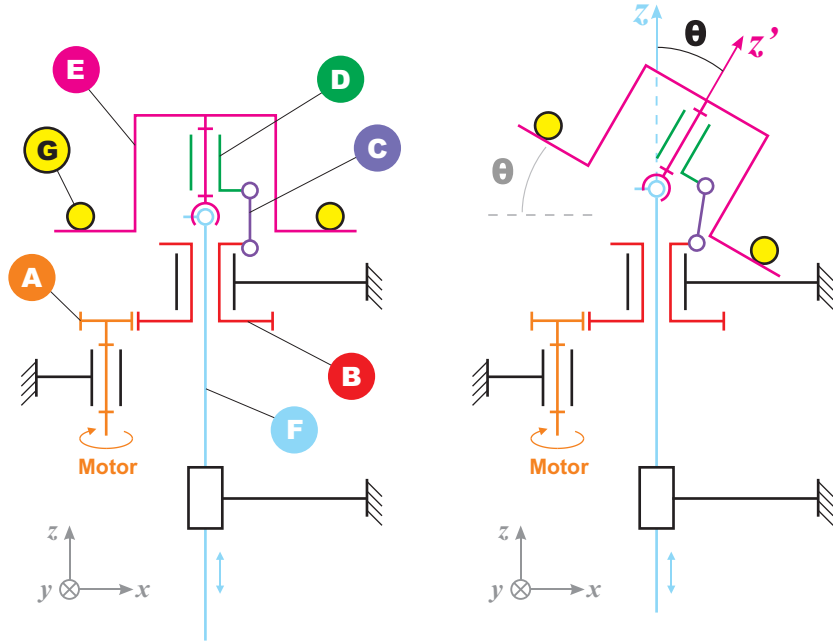


Figure 4: A simplified kinematic diagram illustrates the positions of assemblies of the 3RFL at the horizontal and inclined cases. A: Driveshaft / B: Rotor / C: Connecting rod / D: Slave rotor / E: platform / F: Central shaft / G: Torus tube.

228 camera is aligned with the centre line of the ring loop and positioned at a
 229 distance of 1 m from the outer side of the tube, while the light source is
 230 placed behind the tube as illustrated in Fig. 3. Given that the action camera
 231 is rotating around the ring loop, it is not possible to use the two cameras
 232 together, thus we present here results from the high-speed camera only.

233 A simplified schematic diagram of the 3RFL is given in Fig. 4. It illus-
 234 trates the position of 3RFL elements at horizontal (left panel, $\theta = 0$) and
 235 tilted (right panel, $\theta = 45^\circ$) positions. One may notice that the rocking an-
 236 gle θ corresponds to the angle between the platform and the x - y plane. The
 237 rocking angle of the platform is governed by the position of the central shaft
 238 (F in Fig. 4) along the z -axis. This is possible as (i) the platform and the
 239 central shaft are connected by a universal joint (Fig. 5), (ii) the rotor (B in
 240 Fig. 4) and the slave rotor (D in Fig. 4) are linked by the connecting rod
 241 (C in Fig. 4). The universal joint is given in Fig. 5, and consists of two yokes
 242 attached by the cross-piece. The top yoke (red) is attached to the slave rotor,

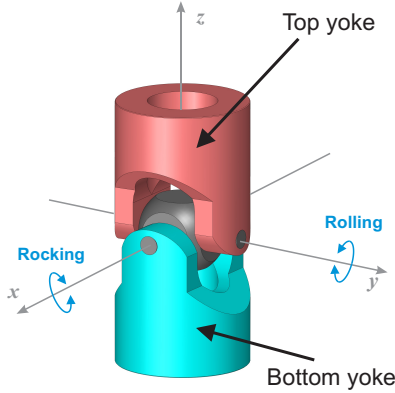


Figure 5: An illustration of the universal joint used in the 3RFL consisting of the top and bottom yokes and a cross-piece in between. The top yoke performs rockings along the x -axis and rollings along the y -axis, while the bottom yoke is motionless

243 while the bottom yoke (blue) is attached to the top end of the central shaft.
 244 The bottom yoke is motionless, whereas the top yoke manoeuvres easily in
 245 the x and y axes (the rotation around the z -axis is prevented). Notably, the
 246 top yoke rocks along the x -axis and rolls along the y -axis. Given that the
 247 slave rotor and the platform are linked, the inclination of the platform is due
 248 to the connecting rod (C in Fig. 4), which compensates for the displacement
 249 of the shaft by pulling the slave rotor (B in Fig. 4) down. As a result, the po-
 250 sition of the connecting rod determines the location of the lowermost part of
 251 the platform and of the ring loop. In practice, the platform tilting is powered
 252 by the electrical motor shown in Fig. 4. The electrical motor (3-phase AC
 253 asynchronous motor, HPC Europe) induces the rotation of the drive shaft
 254 (A in Figs. 2, 4). Then, the rotation of the drive shaft is transmitted to
 255 the rotor (B in Fig. 4) by means of gears. The connecting rod is attached
 256 to the rotor by one end and loosely attached to the slave rotor by another
 257 end. As a result, the connecting rod rotates with the rotor while pulling
 258 down the sequential parts of the periphery of the slave rotor. Thus, the ro-
 259 tational motion of the drive shaft is transformed into rocking and rolling of
 260 the platform.

261 In this regard, Fig. 6 displays the interplay between the rotation of the
 262 rotor and the position of the ring loop. For clarity, the reference frames of
 263 the bottom and top yokes are defined as (x, y, z) and (x', y', z') , respectively,
 264 and the axis length is taken equal to the ring loop radius. When the drive

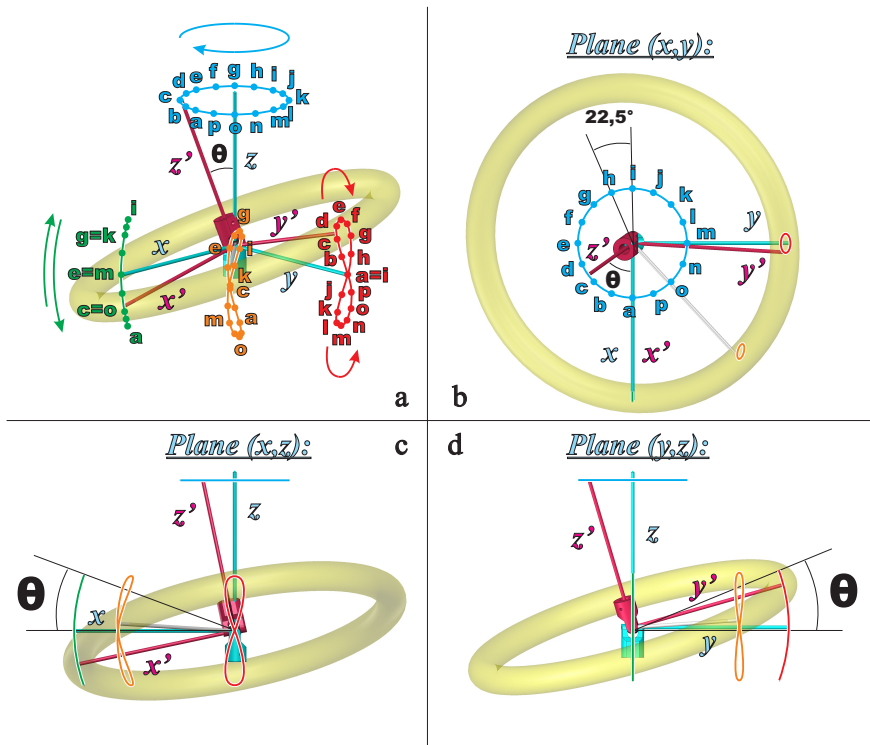


Figure 6: The sketch shows the positions of the ring loop corresponding to the positions of the upper yoke while performing a single tour about the z -axis at an inclination angle θ . Different views are shown: (a) general, (b) in the plane (xy) , (c) in the plane (xz) and (d) in the plane (yz) .

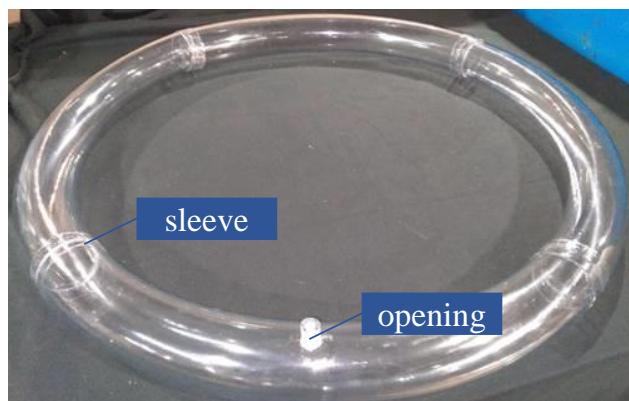


Figure 7: Cellulose acetyl butyrate tube with a diameter of $d = 69.85$ mm with one opening for fluid loading. Sleeves are made to strengthen tube connections.

265 shaft (A in Fig. 4) rotates, the central axis (Oz') of the top yoke draws a cone
 266 of half-angle θ around the bottom yoke central axis (Oz). The top yoke and
 267 the platform share the same central axis (Oz'). Also, the axial line of the
 268 ring loop is aligned with the center of the universal joint ball. To illustrate
 269 via Fig. 6 the interplay between the positions of the yoke and of the ring flow
 270 loop, 16 points (marked in blue as $a - p$) are picked up along the trajectory
 271 followed by the z' -axis corresponding to a complete revolution (360°) of the
 272 rotor (the baseline of the cone in blue). The corresponding trajectories of the
 273 x' - and y' -axis are marked by green and red lines, respectively. The x' tip
 274 draws an arc, which yields the rocking motion. Meanwhile, the y' tip draws
 275 an eight-shape trajectory whose centre coincides with the tip of the y -axis.
 276 The eight-shape movement results in the rolling motion. In this way, the
 277 successive variations of the ring loop position cause fluids to circulate along
 278 the tube.

279 The employed ring loop, shown in Fig. 7, is made of cellulose acetyl
 280 butyrate (CAB) and has one opening for injecting and draining the test
 281 fluids. The optical clarity of the CAB tube allows an easy flow observation
 282 in any part of the system, while its physical strength ensures the stability of
 283 the loop throughout the experiments. The CAB ring loop comprises four 90°
 284 bend tubes solvent welded together. The tube connections are additionally
 285 strengthened by CAB sleeves (Fig. 7). The resulting ring loop dimensions
 286 are provided in Table 2.

287 *2.2. Experimental procedure*

288 The flow experiments aim to characterize air-water flow regimes and iden-
289 tify the emergence of specific flow patterns based on system control paramete-
290 rs. The 3RFL depicted in Fig. 2 is employed to conduct flow experiments
291 at ambient temperature and atmospheric pressure. Flow regimes are de-
292 termined based on direct observation of flow structure within a transparent
293 tube. Certainly, a more advanced experimental methodology might be devel-
294 oped, and superior experimental methods (confocal laser sensor, capacitance
295 probe, . . .) might be introduced in the 3RFL apparatus. However, we would
296 like to stress here that the aim of our work is to build a novel and compact
297 experimental apparatus to mimic multiphase flows for petroleum engineering,
298 *e.g.* under pressure, multiphase and reactive environment (formation of gas
299 hydrates at the water-gas-oil interface). Clearly, the employment of alterna-
300 tive and more advanced experimental methods should be carefully handled
301 given the harsh experimental conditions ($P > 80$ bar and $T < 4^\circ$) we aim
302 at reproducing in future. Indeed such an analysis is under consideration for
303 future studies.

304 To enhance flow visualization, blue methylene powder ($\rho = 1310$ kg/m³;
305 Sigma-Aldrich) is added to water ($\rho = 998.23$ kg/m³, $\mu = 1.002$ mPa s) in
306 a proportion of 1 mg per 1 litre. Coloured water is then loaded into the
307 3RFL through the opening with the aid of a syringe, while the residual air
308 ($\rho = 1.2$ kg/m³, $\mu = 0.01813$ mPa s) in the ring loop is considered the gas
309 phase. Table 2 lists the range of variation of control parameters employed in
310 the experimental campaign.

311 The flow experiment is initiated by manually adjusting the rocking angle
312 using a turning nut and hand wheel (H and I in Fig. 2). The rocking rate
313 is controlled by adjusting the power input of the electric motor, which is
314 then turned on. To analyze the impact of each particular control parameter
315 on air-water flow regimes, the one-factor-at-a-time approach is employed.
316 This approach consists in modifying one control parameter while keeping two
317 others fixed and repeating the process for each of the control parameters.

318 Flow regime observations are carried out when the flow becomes fully
319 developed. Our experiments showed that flow regime becomes fully devel-
320 oped after 2 – 4 full revolutions of the liquid around the ring loop, which
321 corresponds to 6 – 30 seconds based on the rocking rate. We take advantage
322 of the flow loop transparency and the high-speed camera to record the ex-
323 periments on video and verify flow observations. The observed flow regimes
324 are categorized and plotted on a flow regime map.

Control Parameters	Notation	Unit	Range
Rocking rate	f_R	opm	5.81-33.34
Rocking angle	θ	$^\circ$	1-15
Diameter of the ring	D	mm	840
Diameter of the tube	d	mm	69.85
Liquid volume fraction	φ_L	-	0.03-0.15

Table 2: Range of control parameters used during the experiments.

325 To analyse average liquid height and average air bubble diameter, flow
326 videos are converted into image sequences using the ImageJ software. As
327 shown in the top left panel of Fig. 8, from 4 to 7 sub-images are selected
328 from each image sequence to reproduce the lateral view of the liquid over
329 subsequent regions. Liquid height and bubble diameter measurements are
330 carried out using a ruler tool. As the only known distance is the tube diame-
331 ter, this is used as the system’s calibrating parameter. In addition, repeated
332 measurements (228 measurements) of the diameter d_{cam} across flow images
333 were taken to account for optical distortions caused by the tube’s curvature
334 and rocking motion.

335 As shown in the top-right panel of Fig. 8, to analyse the local liquid height,
336 the distance between the gas-liquid interface and the bottom of the tube is
337 measured and denoted as h_{cam} . From each image, at least 10 measurements
338 were taken for a total of 40-90 measurements per flow case. For flow pattern
339 displaying air bubbles, those are manually detected and sized (d_b) as shown
340 in the bottom panel of Fig. 8. Experimental uncertainty measurements is
341 described in section 2.3.

342 According to experimental investigations on two-phase flow in coiled
343 tubes in the literature, we expect that the curvature-induced centrifugal force
344 will drive the heavier phase, *i.e.* the liquid phase, towards the outer wall (O),
345 as depicted in the top right panel of Fig. 8. As the flow images for liquid
346 height measurements are taken from the outer wall, there is a possibility of
347 a measurement discrepancy, as the local liquid height value (h_L), red line)
348 could be smaller than h_{cam} . Therefore, it is crucial to establish the rela-
349 tionship between h_{cam} and h_L accounting for the potential impact of tube

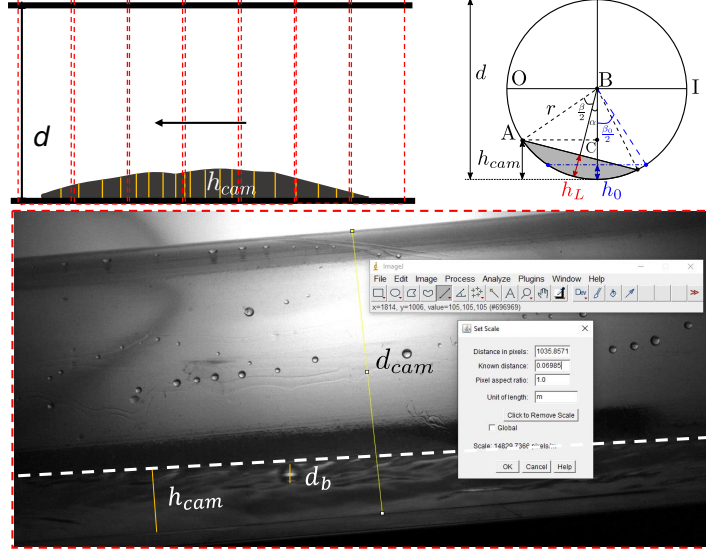


Figure 8: A sketch of the liquid height (h_L) and bubble diameter (d_b) measurement procedure. The red rectangles (top left panel) correspond to one image in the sequence. The bottom panel presents a random flow image in the software interface where d_{cam} is the tube diameter and h_{cam} is the local liquid height.

350 curvature.

351 For this, we introduce the hydraulic angle β (Fig. 8), which corresponds
 352 to an angle whose vertex is at the centre of the tube cross section and whose
 353 arms are radii intersecting two distinct points, where the liquid film touches
 354 the tube perimeter. In radians, the value of the hydraulic angle is ranged
 355 between 0 (gas-filled pipe) and 2π (liquid-filled pipe). From geometrical
 356 considerations of the circular segment, the liquid height h_L can be expressed
 357 using the hydraulic angle and radius of the tube r :

$$h_L = r(1 - \cos \frac{\beta}{2}) \quad (1)$$

358 To evaluate $\beta/2$, in Fig. 8 we represent a triangle ABC , where AB is equal to
 359 the radius of the tube, AC connects the wall-liquid contact point A with the
 360 vertical centre line of the tube segment by an angle $\pi/2$, and $BC = r - h_{cam}$.
 361 Therefore, Eq. 1 can be rewritten as:

$$h_L = r(1 - \cos(\pi/2 - \arcsin \frac{r - h_{cam}}{r} - \alpha)) \quad (2)$$

362 where α denotes the deviation between the vertical radius and h_{L_i} . Following
 363 Zhu et al. (2019), α can be recovered from the relation between centrifugal
 364 and gravitational forces and reads:

$$\alpha = \arctan\left(\frac{2U_L^2 \cos \theta}{gD}\right) \quad (3)$$

365 where θ is the rocking angle, g is gravitational acceleration, D is the diameter
 366 of the ring loop and U_L is the average liquid velocity. U_L can be defined as
 367 a function of the rocking rate (f_R) of the system and the radius of the ring
 368 loop (R):

$$U_L = \frac{2\pi f_R R}{60} \quad (4)$$

369 This relation is justified by our experiment, where it is found that the periods
 370 of rotation of the liquid phase and of the central shaft are the same despite
 371 the variation in rocking angle and liquid volume fraction. Such that, the tilt
 372 angle (Eq. 3) is a function of the control parameters of the system.

373 In this way, local liquid height h_L is calculated by employing system
 374 control parameters and high-speed camera measurements (h_{cam}). One must
 375 note that: (i) the procedure given in Eq. 2 applies to the case where the
 376 air-water interface is tilted from the horizontal. Otherwise, *i.e.* when the
 377 air-water interface is parallel to the horizontal plane and symmetrical with
 378 respect to the vertical centre line of the tube segment, $h_{\text{cam}} = h_L$. (ii) Eq. 2
 379 is valid only for a flat gas-liquid interface in the cross-sectional area. It will
 380 be shown later (Table 4) that in our 3RFL set-up, the air-water interface in
 381 radial direction is not always flat for all observed flow patterns. However,
 382 although the interface is slightly curved in the cross section, the deviation
 383 from the flat configuration is not very high due to the small rocking angles
 384 adopted here. For instance, when the rocking angle is set to 0° , regardless
 385 of the rocking rate, the loop does not have any motion and thus the fluid
 386 is static. Finally, the average liquid height \bar{h}_L and average bubble diameter
 387 \bar{d}_b were calculated as an arithmetic mean of the corresponding local liquid
 388 height and air bubble diameter values:

$$\bar{h}_L = \frac{1}{n} \sum_{i=1}^n h_{L_i}, \quad \bar{d}_b = \frac{1}{n} \sum_{i=1}^n d_{b_i} \quad (5)$$

389 where h_{L_i} and d_{b_i} are the single measurement.

390 *2.3. Experimental uncertainties*

391 This section presents uncertainty analysis conducted for the measure-
 392 ments of average liquid height (\bar{h}_L) and average bubble diameter (\bar{d}_b). In
 393 compliance with the International Organization for Standardization (ISO),
 394 assessment of uncertainty entails consideration of Type A and Type B un-
 395 certainties (2008ISO/IEC2008). Type A uncertainty arises from repeated
 396 observations, while Type B uncertainty is based on all available information
 397 about the measurand's variability, such as previous measurements, instru-
 398 ment specifications, calibration data, and reference data from handbooks.

399 Given that \bar{h}_L is evaluated as the mean of n independent observations,
 400 Type A uncertainty is estimated as a relation of standard deviation of the
 401 mean to the square root of the number of observations (2008ISO/IEC2008):

$$\mathcal{U}(\bar{h}_L) = \frac{1}{\sqrt{n}} \frac{\sum_{i=1}^n (h_{L_i} - \bar{h}_L)}{\sqrt{n-1}}. \quad (6)$$

402 As noted in the experimental procedure, whether the liquid flow is tilted or
 403 not defines the relation between h_{L_i} and h_{cam_i} . It is notable that Type A
 404 uncertainty varies for each studied case since the tilt angle α and the number
 405 of observations n may change. In the present case, Type B uncertainty stems
 406 from the uncertainty of the tube diameter dimension used for system cali-
 407 bration and instrument uncertainties related to optical distortions (Fig. 8).
 408 We will now assess each of these two uncertainties and then we will inte-
 409 grate them into the combined uncertainty along with Type A uncertainty
 410 calculated based on Eq. 6.

411 We start by assessing the tube diameter uncertainty. The tube diameter
 412 was determined as the average value of 20 measurements conducted using a
 413 Vernier caliper. The uncertainties related to the diameter measurement are
 414 as follows: (i) *Type A* uncertainty, calculated as the standard uncertainty of
 415 the mean, i.e., the population standard deviation divided by the square root
 416 of the number of observations, yielding $\pm 0.003\text{mm}$ (2008ISO/IEC2008):

$$\mathcal{U}(\bar{d}) = \frac{1}{\sqrt{n}} \frac{\sum_{i=1}^n (d_i - \bar{d})}{\sqrt{n-1}}, \quad (7)$$

417 where $\bar{d} = 1/n \sum_i^n d_i$ is the mean value of the tube diameter measurements
 418 and n is the number of measurements; (ii) *Type B* uncertainty, assigned by
 419 instrument accuracy, which is half of the smallest increment of the Vernier

420 caliper, *i.e.*, ± 0.01 mm. The combined uncertainty of the tube diameter,
 421 $\mathcal{U}_c(\bar{d}) = \pm 0.01$ mm, is calculated as the root sum of the squares of Type
 422 A and Type B uncertainties. This total standard uncertainty is associated
 423 with a 68% confidence level. To expand the confidence interval to a 95%
 424 level, a coverage factor of 2 is applied, which is obtained from Student's
 425 t-distribution. Finally, the expanded uncertainty of the tube diameter is
 426 $U(\bar{d}) = \pm 0.02$ mm, corresponding to a 95% confidence level.

427 Uncertainties related to optical distortions from tube curvature, position
 428 variations, and instrument precision were addressed by analyzing 138 images
 429 at a rocking angle of $\theta = 5^\circ$. These images represent all possible variations
 430 in the position of the observed tube segment corresponding to a complete
 431 revolution of the liquid around the loop. This yielded 228 outer diameter
 432 measurements (d_{cam_i}):

- 433 1. 138 values correspond to punctual measurements of the outer diameter
 434 (at the center of the image) to address variations in segment position
 435 due to rocking, as the tube is moving up and down (see for instance
 436 Fig. 10).
- 437 2. 20 values are obtained by moving from left to right within one image
 438 with small increments, aiming to account for optical distortions at the
 439 image edges due to curvature.
- 440 3. 70 values are taken from 14 images (each tenth image), with five equally
 441 spaced measurements from each image to complete the sample.

442 Finally, the standard uncertainty of the mean \bar{d}_{cam} (optical distortion uncer-
 443 tainty) is:

$$444 \mathcal{U}(\bar{d}_{\text{cam}}) = \frac{1}{\sqrt{n}} \frac{\sum_{i=1}^n (\bar{d}_{\text{cam}_i} - \bar{d}_{\text{cam}})}{\sqrt{n-1}} = \pm 0.02 \quad (8)$$

444 where $n = 228$. In contrast to Type A uncertainty, Type B uncertainties of
 445 average liquid height measurement will remain independent of flow conditions
 446 and will be the same for air bubbles diameter measurements.

447 Finally, the combined uncertainty of the average liquid height $\mathcal{U}_c(\bar{h}_L)$ is
 448 then calculated as square root of sum of squares of Type A and Type B
 449 uncertainties:

$$450 \mathcal{U}_c(\bar{h}_L) = \sqrt{\mathcal{U}(h_L)^2 + \mathcal{U}_c(\bar{d})^2 + \mathcal{U}(\bar{d}_{\text{cam}})^2} \quad (9)$$

450 This combined standard uncertainty is associated with a 68% confidence
 451 level. To achieve a 95% confidence level, the resulted \mathcal{U}_c value is multiplied
 452 by 2.

453 The uncertainty of average bubble size measurement comprises Type A
454 uncertainty stemming from repeated measurements and Type B uncertainty,
455 i.e. instrumental uncertainty. Type A uncertainty of the mean is obtained
456 by dividing the standard deviation of the bubble diameter measurements by
457 the square root of the number of observations. As number of detected air
458 bubbles varied wrt. the rocking rate, Type A uncertainty varied. Mean-
459 while, Type B uncertainty remains unchanged with respect to that of liquid
460 height measurements. Finally, the combined uncertainty is estimated as the
461 root of the sum of squares of Type A and Type B uncertainties, then mul-
462 tiplied by a coverage factor equal to 2 to yield an expanded uncertainty, *i.e.*
463 corresponding to 95% confidence level.

464 2.4. Dimensionless parameters of the flow

465 Air-water flow regimes result from the balance of various forces acting on
466 the system and are also affected by pipe geometry and fluid characteristics.
467 We consider gravity, viscous, inertial, surface tension, and centrifugal forces
468 as significant factors in our system. To understand the nature of flow regime
469 transition (see Section 3), we evaluate the dimensionless numbers Reynolds,
470 Weber and Froude based on (Murai et al., 2006). The ratio of inertial to
471 viscous forces is determined by the Reynolds number:

$$Re = \frac{\rho_L h_0 U_L}{\mu} \quad (10)$$

472 where ρ and μ are the density and the dynamic viscosity of the fluid and
473 U_L is the average velocity of the liquid phase. From Fig. 8, h_0 is a reference
474 liquid height, corresponding to the thickness of the liquid film at the centre of
475 the cross-sectional area when the system is static and the ring is horizontal.
476 In other words, it is the maximum film thickness in the section at rest:
477 $h_0 = \max[h(f_R = 0, \theta = 0)] = h_L(f_R = 0, \theta = 0)$. Note that h_0 and h_L are
478 not equal as the liquid might experience de-wetting in the axial direction.
479 The reason why h_0 is chosen as reference scale (rather than the pipe diameter)
480 is mainly due to our two-phase flow, which is not driven by pressure gradient.
481 In this condition, the gas is solely driven by the shear exerted by the liquid.
482 From the geometry of the pipe segment, h_0 may be expressed as:

$$h_0 = r(1 - \cos \frac{\beta_0}{2}) \quad (11)$$

483 where r is the radius of the tube and β_0 is the hydraulic angle when both
484 the rocking rate and the rocking angle are set to zero, in other words β_0 is

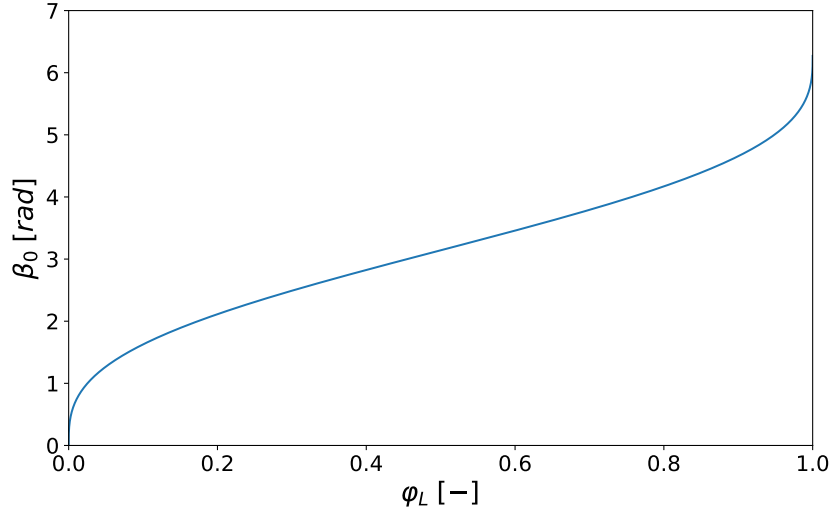


Figure 9: Hydraulic angle at the state of rest of the air-water flow as a function of liquid volume fraction (Eq.14).

485 the angle subtended by the liquid phase in the pipe segment at rest (Fig. 8).
 486 The value of β_0 depends on the volume of the liquid phase, *i.e.* the liquid
 487 volume fraction φ_L . The latter can be expressed as a relation of the area of
 488 the liquid phase in the cross-section of the pipe (A_L) to the total area of the
 489 pipe segment (A_P):

$$\varphi_L = \frac{A_L}{A_P} \quad (12)$$

490 Following Lee et al. (2013), the geometrical parameters in the tube segment
 491 can be expressed in terms of r and β :

$$A_P = \pi r^2 \quad A_L = \frac{1}{2} r^2 (\beta - \sin \beta) \quad A_G = A_P - A_L \quad (13)$$

492 Upon substitution one obtains:

$$\varphi_L = \frac{\beta_0 - \sin \beta_0}{2\pi} \quad (14)$$

493 The solution of Eq. 14 is showed in Fig. 9, which allows to estimate h_0 . Low
 494 Re numbers lead to laminar flow, where viscous forces are not negligible as
 495 in a turbulent flow. Indeed, the laminar flow is mainly characterized by a

Non-dimensional number	Values
Fr	0.25 – 5.47
Re	1287 – 22153
We	5 – 463

Table 3: Range of values of the non-dimensional numbers considered in this study.

496 parallel flow. The relationship between surface tension and inertial forces is
 497 expressed by the Weber number:

$$We = \frac{\rho U_L^2 h_0}{\sigma} \quad (15)$$

498 At low We numbers, the surface tension forces which tend to stabilize the
 499 flow, prevail. The Froude number corresponds to the relation between cen-
 500 trifugal and gravitational acceleration:

$$Fr = \sqrt{\frac{\omega^2 R}{g \sin \theta}} \quad (16)$$

501 where g is the gravitational acceleration, θ is the rocking angle, R is the radius
 502 of the ring and ω is angular velocity. We have also verified that centripetal
 503 forces U_L^2/R are much smaller than gravitational forces and do not affect
 504 the value of g significantly. When the Fr number is high, centrifugal forces
 505 dominate the flow. Table 3 summarizes the Fr , Re and We values calculated
 506 for the studied system. An analysis of such values, $Re > 1$ and $We > 1$,
 507 indicates that inertial forces dominate over viscous and surface tension forces.
 508 Meanwhile, Fr values ranging from 0.25 to 5.47 indicate that depending on
 509 the flow conditions, gravitational or centrifugal forces may prevail.

510 3. Experimental results

511 3.1. Observed air-water flow regimes

512 Varying system control parameters such as the rocking angle θ , rocking
 513 rate f_R , and liquid volume fraction φ_L resulted in different air-water flow
 514 regimes. Based on visual observations, three flow regimes are identified such
 515 as smooth interrupted, wavy-bubbly continuous and smooth continuous. Ta-
 516 ble 4 provides illustrations of the observed flow regimes as seen from both

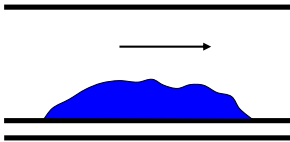
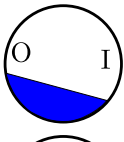
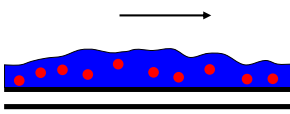
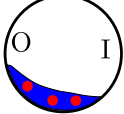
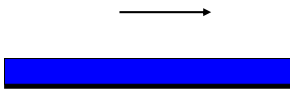
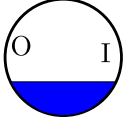
Flow Regime	Stream-wise sketch	Radial sketch
Smooth Interrupted (SI)		
Wavy-Bubbly Continuous (WBC)		
Smooth Continuous (SC)		

Table 4: Air-water flow regimes observed in the 3RFL.

517 a stream-wise and radial perspective. Flow images of corresponding flow
518 regimes are given in Fig. 10. For better comprehension, you may refer to the
519 videos of flow regimes in the supplementary materials.

520 The Smooth Interrupted (SI) regime defines the configuration for which
521 the liquid flows at the bottom of the tube in the form of a hump (A in
522 Fig. 10) while the rest of the tube is dewetted. Notably, this hump flows
523 following the lowermost part of the ring loop during successive rockings and
524 rolling, meaning that the downward gravity is a driving force of the flow.
525 The gas-liquid interface is mainly smooth or has ripples. Depending on the
526 rocking rate flow can be symmetrical and asymmetrical with respect to the
527 vertical centre line of the tube cross section.

528 The Wavy-Bubbly Continuous (WBC) regime identifies the flow config-
529 uration for which the bottom of the tube is fully wetted in its length and
530 the gas-liquid interface is wavy-bubbly (B in Fig. 10). Meanwhile, as shown
531 in Table 4, during WBC, the gas-liquid interface is asymmetrical with re-
532 spect to the vertical diameter of the tube cross-section. Indeed, the level of
533 liquid at the outer wall is higher than at the inner wall. Following Murai
534 et al. (2006); Banerjee et al. (1969) this can be explained by the effect of
535 curvature-induced centrifugal force which pushed the dense phase, *i.e.* liquid
536 phase, towards the outer wall. Flow images of wavy-bubbly continuous flow
537 allowed us to characterize air bubble behaviour throughout the flow. It is
538 observed that air bubbles have a spherical shape. We suggest that bubbles

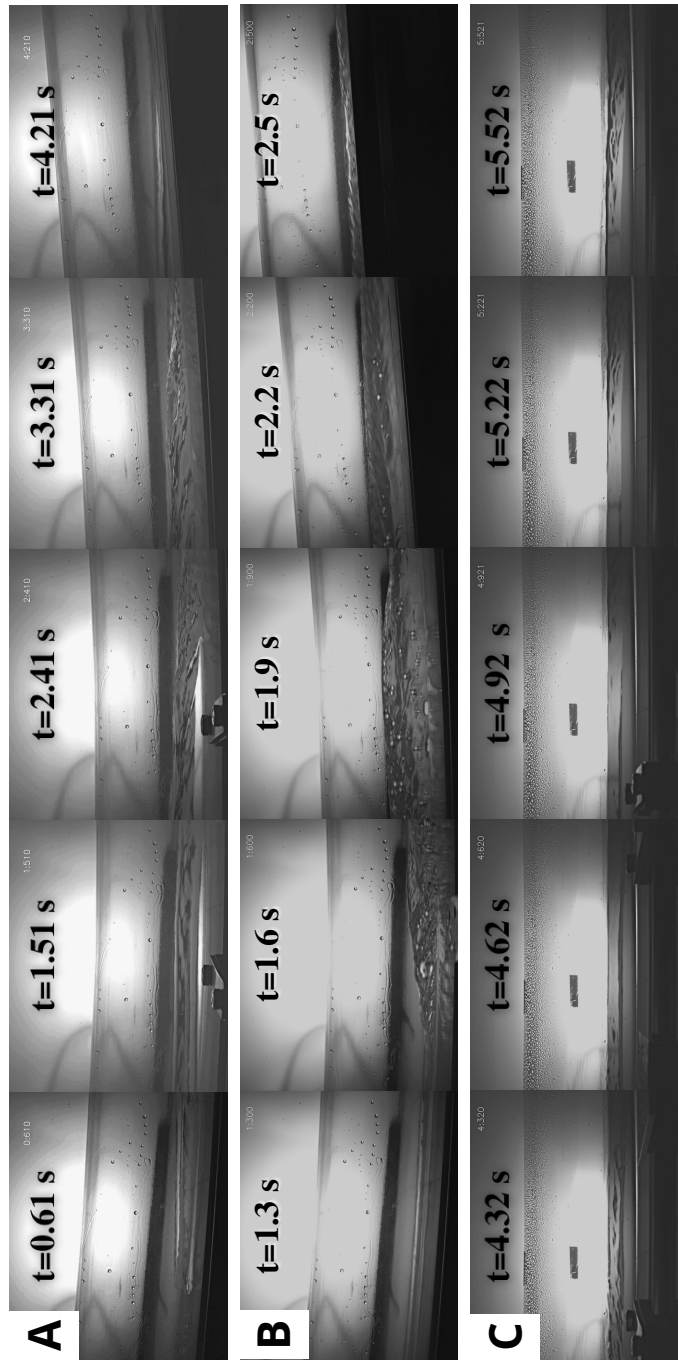


Figure 10: Air-water flow regimes: (A) smooth interrupted, (B) wavy-bubbly continuous and (C) smooth continuous.

539 entrap into the liquid phase due to the curvature-induced secondary flow.
 540 The secondary flow is characterized by the migration of the fluid from the
 541 inner side of the tube toward the outer wall by tube walls and returning to
 542 the inner wall by the horizontal central line (Dean, 1927). This initiates ra-
 543 dial mixing, causing some parts of the liquid phase to collide with each other
 544 in the presence of air, resulting in the entrainment of air within the liquid.
 545 Besides, the radial mixing promotes air bubble collisions, which leads to their
 546 flocculation and coalescence. This observation is consistent with Kaji et al.
 547 (1984) and Murai et al. (2006). From our observations, bubbles are able to
 548 grow into agglomerated structures that subsequently dissociate (see video 5
 549 in supplementary materials). The analysis of air bubble size and distribution
 550 will be conducted in Section 3.4.

551 The Smooth Continuous (SC) regime corresponds to the flow structure
 552 for which the liquid is uniformly distributed over the entire length of the
 553 ring. Here the elevation of the liquid is the same all along the pipe, despite
 554 the successive tilting of the ring loop (C in Fig. 10). In some way, such flow
 555 behaviour recalls the wall-clinging effect described by Murai et al. (2006) for
 556 which the liquid bulk is forced to reside at the bottom of the tube due to
 557 the strong influence of centrifugal forces on the system. Meanwhile, the gas-
 558 liquid interface is smooth or may have ripples. Also, the flow is symmetrical
 559 in the radial cross-sectional area. Now we analyse the impact of system
 560 control parameters on flow regime occurrence.

561 3.2. Effect of system control parameters on flow regimes

562 In Fig. 11, the flow regime maps for the observed air-water flow regimes
 563 in the 3RFL with a diameter of $d = 69.85$ mm are shown. The liquid volume
 564 fraction (φ_L) is represented on the x -axis, while the rocking angle (θ) is
 565 represented on the y -axis. The ten panels correspond to different values of
 566 the rocking rate f_R . The flow regime boundaries are indicated by a black
 567 dashed line. The blue triangles, red circles, and grey squares in the figure
 568 indicate the smooth interrupted (SI), wavy-bubbly continuous (WBC), and
 569 smooth continuous (SC) regimes, respectively. The green stars correspond
 570 to flow regimes difficult to identify as either SI or WBC.

571 At small rocking rates ($f_R \leq 8.51$ opm, panels in the first line), mainly
 572 the SI regime occurs for all θ and φ_L . As the rocking rate increases ($9 <$
 573 $f_R < 14$ opm, panels in the second line), the WBC regime starts to occur
 574 at low θ for each considered φ_L . By further increasing f_R ($f_R = 16.78$ opm,
 575 fifth panel), the SC regime occurs now at low θ for each φ_L , whereas the

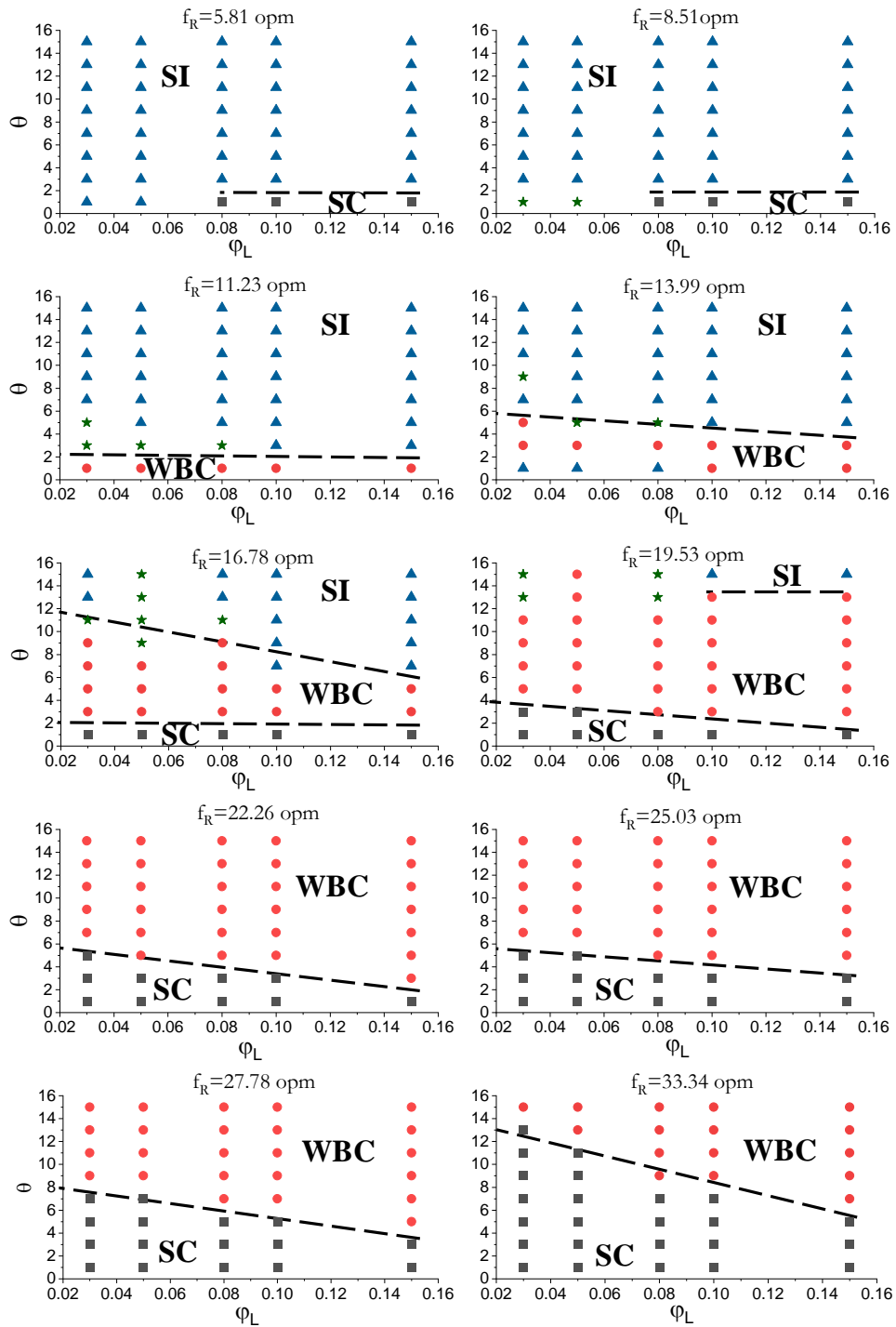


Figure 11: Air-water flow regime map.

576 WBC regime expands at larger θ , leading to the SI regime to disappear
577 ($f_R = 22.26$ opm, seventh panel). At even larger values of f_R ($f_R > 23$ opm,
578 eighth to tenth panel), the SC regime occurs at larger θ and widens.

579 Flow regime transition boundaries are also governed by inclination angle
580 and volume fraction. As the liquid volume fraction increases, SI-WBC and
581 WBC-SC transitions take place at smaller rocking angles. The combination
582 of low rocking angles, high rocking rates, and high liquid volume fraction
583 leads to an increased effect of the gravity force, promoting a smooth inter-
584 rupted flow. As the rocking rate rises, the influence of centrifugal forces on
585 the flow becomes more pronounced. This causes some liquid to accumulate
586 at the bottom of the tube, transitioning the flow from an interrupted regime
587 to a continuous one, such as smooth continuous (SC) or wavy-bubbly con-
588 tinuous (WBC) flow. In particular, the WBC flow regime arises when liquid
589 loading, rocking rate, and angle are large, whereas when the rocking rates are
590 high, and the rocking angles are low ($\theta=1-5^\circ$), centrifugal forces overcome
591 gravity, leading to the occurrence of the SC regime. In what follows, flow
592 regime transitions will be analysed using previously defined dimensionless
593 parameters of the flow.

594 Figure 12 collects all the experimental data obtained by varying the con-
595 trol parameters as in Table 2. In particular, Figure 12 shows the flow regime
596 maps in the $Fr-We$ plane (top panel) and in the $Fr-Re$ plane (bottom panel).
597 Again, blue triangles indicate smooth interrupted (SI), red circles indicate
598 wavy-bubbly continuous (WBC) and grey rectangles indicate smooth contin-
599 uous (SC) regimes. Flow regimes which are questionable to identify as SI or
600 WBC are marked by green stars. Flow regime boundaries are shown by black
601 dashed lines. Flow regime transition boundaries have a steep slope, which
602 indicates that they are highly dependent on the value of the Fr number.
603 This suggests that the relation between centrifugal and gravitational forces
604 plays a crucial role in the appearance of a particular flow regime. Indeed,
605 when the flow is mainly governed by the gravity force, *i.e.* when $Fr < 1$,
606 the smooth interrupted flow is promoted (blue triangles). As the centrifu-
607 gal force is dominant over gravity ($Fr > 2$), the flow is smooth continuous
608 (grey rectangles). This can be attributed to the centrifugal force-promoted
609 wall-clinging effect reported in literature (Murai et al., 2006; Akagawa et al.,
610 1971). Now, the total liquid volume is evenly distributed throughout the
611 loop.

612 In the intermediate region where $1 < Fr < 2$, there exists a competi-
613 tion between gravity and centrifugal forces, leading to an intermediate and

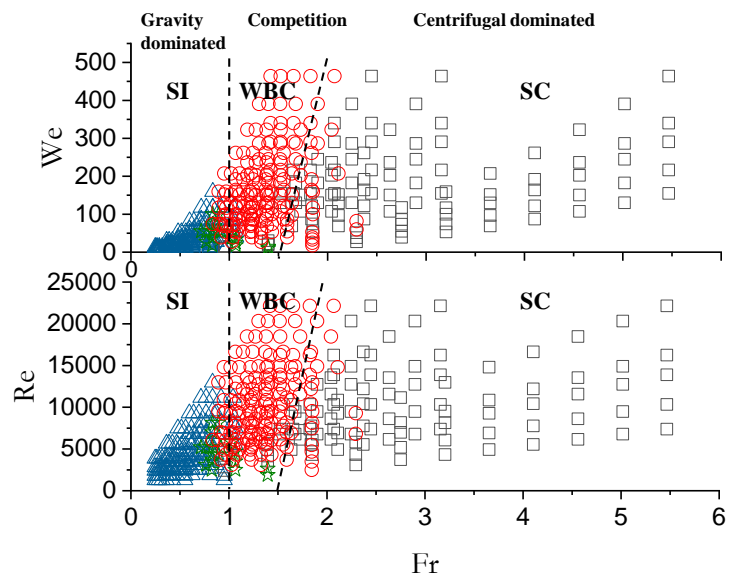


Figure 12: Flow regime map ($Fr - We$) (top) and ($Fr - Re$) (bottom) of air-water two-phase flow in the 3RFL with $d = 69.85$ mm. SI regime - blue triangles, WBC regime - red circles, SC regime - grey rectangles and there are controversial cases marked by green stars, where the regimes are either SI or WBC.

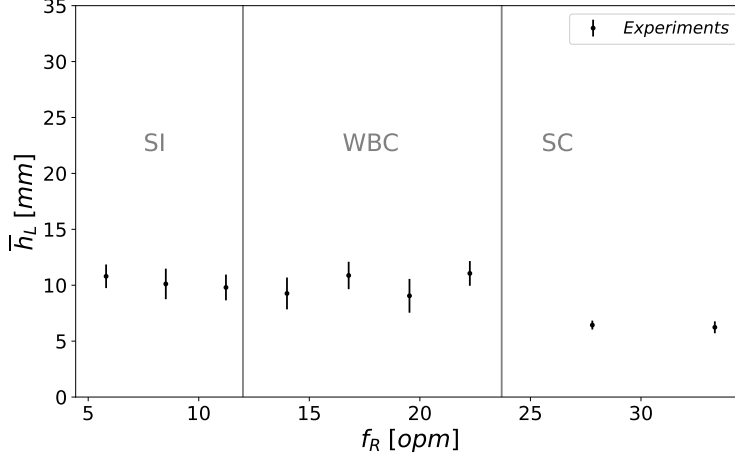


Figure 13: Results of the liquid height measurements for the air-water flow in 3RFL with $d=69.85$ mm, $\varphi_L = 0.05$, $\theta = 5^\circ$ and different rocking rates.

614 disturbed wavy-bubbly continuous (red circles) flow.

615 3.3. Liquid height measurements

616 To compare the experimental results to the different modelling strategies
617 (section 4.4), we present here the experimentally obtained liquid heights. In
618 Fig. 13 results for the average liquid height h_L are shown (black dots) as a
619 function of rocking rate, by accounting for the measurement error, through
620 error bars, as described earlier. The chosen configuration consists of $\varphi_L =$
621 0.05 and $\theta = 5^\circ$. Grey vertical lines refer to the flow regime boundaries,
622 as observed experimentally. By comparing the liquid height values for SI
623 and SC regimes, one may notice that the layer of the liquid thins for the
624 latter. Meanwhile, for the WBC regime, the average height of the liquid is
625 almost the same as the SI regime or slightly increases with the rocking rate
626 f_R . The reason for this increase is twofold. First, the presence of air bubbles
627 entrapped inside the liquid layer finally raises the level of the liquid. Secondly,
628 the centrifugal force pushes the liquid towards the outer wall causing the
629 asymmetry of the level of the interface. Therefore, the height of the liquid
630 level on the outer side is higher than on the inner side (see Table 4). Given
631 that analysed images are taken from the outer wall explains the discrepancy.

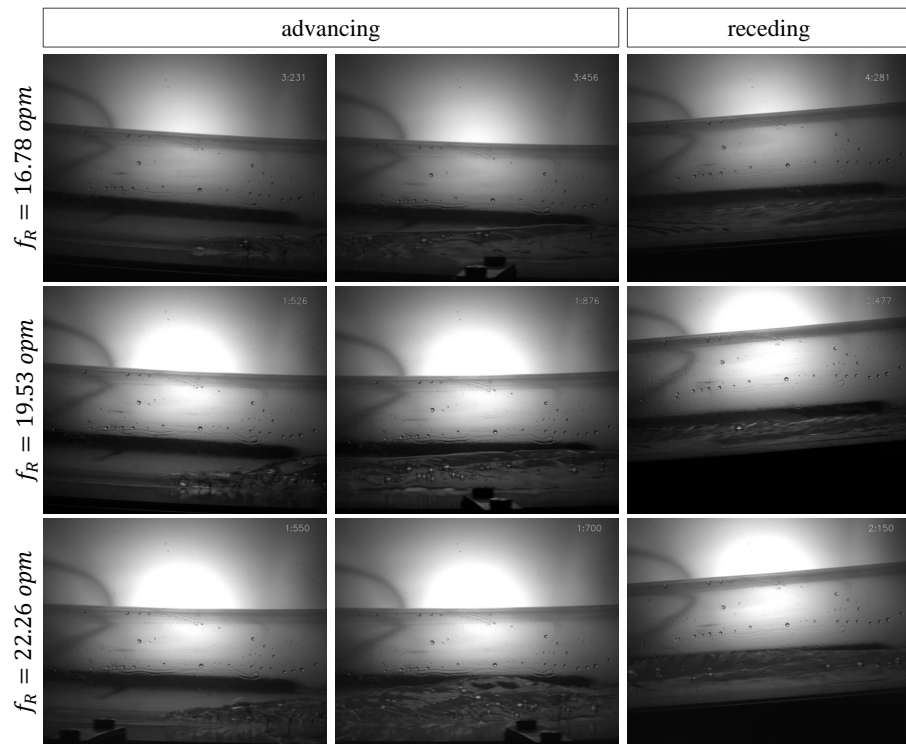


Figure 14: Images of advancing and receding parts of the air-water bubbly flow at various rocking rates: $f_R = 16.78 \text{ opm}$ (1st row), 19.53 opm (2nd row), and 22.26 opm (3rd row).

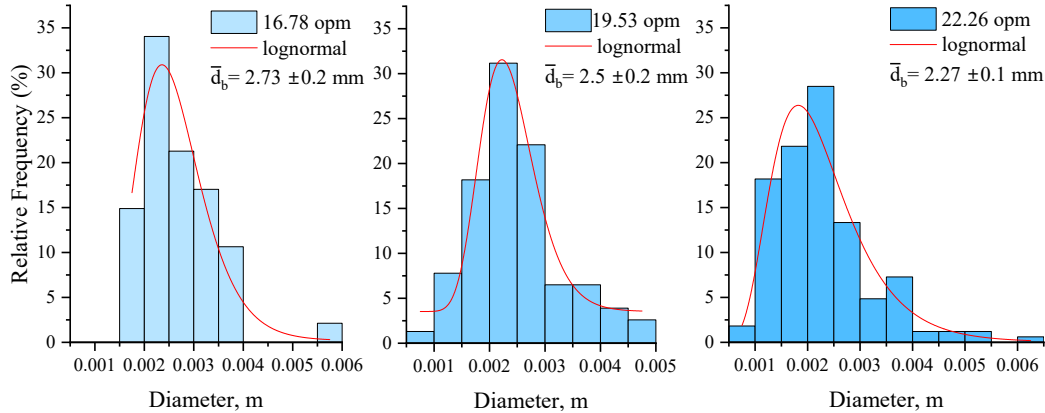


Figure 15: Results on the relative frequency of bubble size estimated for the air-water bubbly flow in 3RFL with $d = 69.85$ mm with $\varphi_L = 0.05$, $\theta = 5^\circ$ and $f_R = 16.78$ opm (left panel), 19.53 opm (central panel) and 22.26 opm (right panel). A curve in red is a log-normal curve.

632 3.4. Air bubbles size and distribution

633 Fig. 14 demonstrates flow images of different parts of the wavy-bubbly
 634 continuous flow, *e.g.* the advancing and receding parts, at $\theta=5^\circ$, $\varphi_L = 0.05$
 635 and various rocking rates including $f_R = 16.78$ opm, 19.53 opm, and 22.26
 636 opm. It is noticed that the air bubbles in the WBC flow are non-homogeneous
 637 in terms of size and distribution. In regard the distribution, it is observed
 638 that the main volume of bubbles is concentrated in the advancing part of the
 639 flow, while the receding part of the flow contains few or no bubbles. Besides,
 640 in Fig. 14, one may note that an increase in the rocking rate produces more
 641 bubbles meaning that the secondary flow becomes more pronounced.

642 Now, we focus on the results of the bubble size analysis obtained by image
 643 processing. Fig. 15 displays the relative frequency of bubble size distribution
 644 at various rocking rates. As one may note, the bubble size distribution fits
 645 into the log-normal curve (red line, Fig. 15). With an increase in the rocking
 646 rate, the number of detected bubbles increased from 47 (for $f_R = 16.78$
 647 opm) to 165 ($f_R = 19.53$ opm), which justifies our observations. However,
 648 it is found that the mean diameter \bar{d}_b decreases with the rocking rate. This
 649 shows that the more bubbles are entrapped, the more they are fractured.

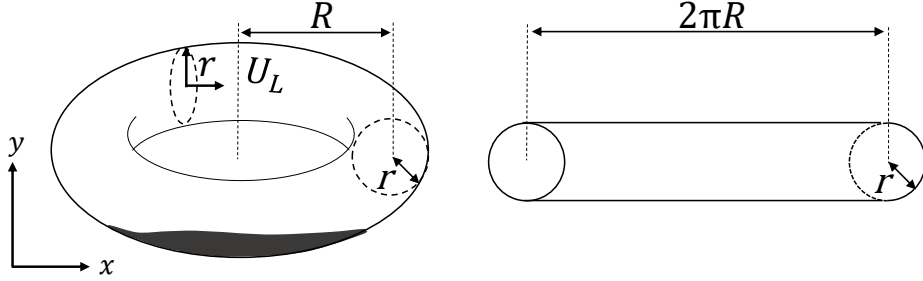


Figure 16: Sketch of the horizontal ring loop, where r is the radius of the tube and R is the radius of the ring, and U_L is the average velocity of the liquid phase.

650 **4. Air-water flow modelling and validation**

651 As shown in Fig. 13, the experimental analysis provides the average liq-
 652 uid heights in the 3RFL for all studied flow regimes. We now complement
 653 the experimental analysis with modeling development, which might be help-
 654 ful to study the effect of varying fluid properties and flow conditions, *e.g.*
 655 replacing water with oil. Therefore, in this section we focus on the devel-
 656 opment of a modelling strategy for the investigation of the air-water flow
 657 within the 3RFL. Three modelling approaches are applied to predict the av-
 658 erage height of the liquid level h_L for the studied flow: mechanistic model,
 659 total energy minimization model and a combined approach. To begin with,
 660 we approximate the ring loop as a horizontal pipe as illustrated in Fig. 16.
 661 With this in mind, as shown in Fig. 17, we consider a downward inclined
 662 tube in which gas-liquid flow is driven by gravity and by an external force
 663 related to the rotation of the shaft. The liquid phase flows at the bottom of
 664 the conduit as heavier fluid. Also, we presume that the flow is incompressible
 665 and steady-state.

666 Before pursuing with the model development, it is noteworthy to mention
 667 that the final goal is to obtain modelled average liquid heights to compare
 668 to those obtained experimentally. Note that liquid heights h_L and hydraulic
 669 angles β are linked in a unique way (see Fig. 8 and Eq. 1). For this, for
 670 each of the three adopted modeling strategy, we have developed an equation
 671 solely enslaved to the hydraulic angle β . While expressing the areas occupied
 672 by the liquid and the gas, as well as the average liquid and gas velocities as
 673 a function of β is straightforward - as it will be shown later - this is not
 674 the case for the wall shear stresses, unless computed via empirical relations.

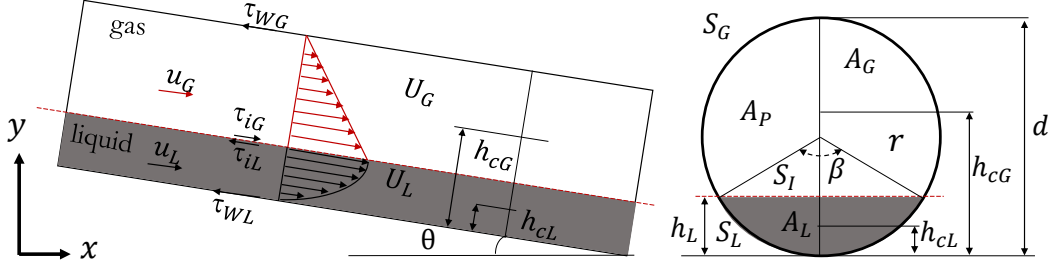


Figure 17: Sketch of the gas and liquid flow and velocity profiles in an inclined channel. Subscripts G , L and I denote gas, liquid and interface, d is the diameter of the tube, θ is pipe inclination angle, A is the area, S is the contact perimeter, h is height, U is average velocity, and u is velocity profile.

675 Therefore, closure relations are needed to express viscous terms as a function
 676 of β only. One way to accomplish this consists in deriving the liquid and gas
 677 velocity profiles, and then derive those to find the wall shear stresses. By
 678 assuming that the gas-liquid interface remains flat, the liquid velocity u_L
 679 is uniform in the stream-wise direction, thus $u_L = u_L(y)$. Also, the velocity pro-
 680 file is parabolic given the equilibrium between volumetric and viscous forces
 681 (Nusselt, 1916). Furthermore, since there is no applied pressure gradient, we
 682 suppose that the gas flows along the tube only due to the entrainment of the
 683 liquid layer. As a result, the gas velocity profile u_G is linear with the coordi-
 684 nate y , and in a similar way as the liquid, the gas velocity is uniform in the
 685 stream-wise direction, hence $u_G = u_G(y)$. Assuming no-slip velocity at tube
 686 walls, continuity of velocities and shear stresses at the gas-liquid interface as
 687 boundary conditions, one can obtain gas and liquid velocity profiles:

$$u_G = \frac{6U_L(d - y)}{h_L(\mu_G/\mu_L + 4d/h_L - 4)} \quad (17)$$

688 and

$$u_L = \frac{6U_L}{h_L^2} \frac{(1 - d/h_L - \mu_G/\mu_L)}{(\mu_G/\mu_L + 4d/h_L - 4)} y^2 + \frac{6U_L(\mu_G/\mu_L + 2d/h_L - 2)}{h_L(\mu_G/\mu_L + 4d/h_L - 4)} y \quad (18)$$

689 where the condition for the average velocity $U_L = 1/h \int_0^{h_L} u_L(y)$ has been
 690 also employed. In Eqs. (17) and (18), d is the diameter of the tube, μ_G and
 691 μ_L are gas and liquid viscosities, h_L is the height of the liquid level. Note

692 that h_L is still unknown. By definition of the flow within a conduit, U_L
 693 can be determined as a relation of the volumetric liquid flow rate Q_L to the
 694 cross-sectional area occupied by the liquid phase A_L :

$$U_L = \frac{Q_L}{A_L} \quad (19)$$

695 where $Q_L = V_L/t$, being V_L is the liquid volume within the pipe. As for the
 696 time t , we verified that the period of circulation of the liquid phase is equal
 697 to the rotational period of the rotor $60/f_R$. Thus, average velocity U_L reads:

$$U_L = \frac{V_L f_R}{A_L 60} \quad (20)$$

698 Again, U_L depends on the area occupied by the liquid, which is unknown as
 699 it depends on h_L (Eq. 13 and 1).

700 We are also interested in determining the wall and interfacial shear stresses.
 701 These can be derived either through empirical correlations or by derivation
 702 of the velocity profiles Eqs. (17) and (18). The latter leads to:

$$\tau_{WL} = \mu_L \left. \frac{du_L}{dy} \right|_{y=0} = \frac{6U_L}{h} \frac{\mu_L(\mu_G/\mu_L + 2d/h - 2)}{\mu_G/\mu_L + 4d/h - 4} \quad (21)$$

$$\tau_{WG} = \tau_{iG} = \mu_G \left. \frac{\partial u_G}{\partial y} \right|_{y=h} = -\frac{6U_L}{h} \frac{\mu_G}{\mu_G/\mu_L + 4d/h - 4} \quad (22)$$

$$\tau_{iG} = \mu_G \left. \frac{\partial u_G}{\partial y} \right|_{y=h} \quad (23)$$

705 It comes out that the interfacial and the gas shear stresses are uniform and
 706 constant, whilst the liquid shear stress is linear with the cross-stream coordi-
 707 nate. Noteworthy is that velocity profiles (Eqs. 17 - 18) and shear stresses
 708 (Eqs. 21- 22) are functions of the fluid properties, tube diameter, position of
 709 the interface h_L (Eq. 1) and average velocity of the liquid phase U_L (Eq. 20).
 710 Now, h_L and U_L are functions of the variable parameter β . Therefore, the
 711 problem has been restructured as solely the hydraulic angle β remains as the
 712 parameter and all other quantities can be enslaved to β . In what follows,
 713 the mechanistic and the total energy minimization model as well as a com-
 714 bined approach will be applied to the above-described problem to predict the
 715 gas-liquid flow arrangement in terms of h_L (or β).

716 *4.1. Mechanistic model*

717 Considering the flow configuration described in Fig. 17, and following Tai-
 718 tel and Dukler (1976b) assumptions, the momentum conservation equations
 719 for each phase are:

$$-A_G \left(\frac{dP}{dx} \right)_G - \tau_G S_G + \tau_I S_I + \rho_G g A_G \sin \theta = 0 \quad (24)$$

720

$$-A_L \left(\frac{dP}{dx} \right)_L - \tau_L S_L - \tau_I S_I + \rho_L g A_L \sin \theta = 0 \quad (25)$$

721 where $\left(\frac{dP}{dx} \right)_G$ and $\left(\frac{dP}{dx} \right)_L$ are pressure gradients in the gas and in the liquid
 722 phases, whereas τ_G , τ_L , and τ_I are gas-wall, liquid-wall and gas-liquid inter-
 723 facial shear stresses. Finally, g is gravitational acceleration, ρ_G and ρ_L are
 724 densities of the gas and the liquid phases, whereas θ is the inclination angle of
 725 the tube from the horizontal. From the momentum conservation one yields:

$$-\left(\frac{dP}{dx} \right)_G = \tau_{WG} \frac{S_G}{A_G} - \tau_I \frac{S_I}{A_G} - \rho_G g \sin \theta \quad (26)$$

726

$$-\left(\frac{dP}{dx} \right)_L = \tau_{WL} \frac{S_L}{A_L} + \tau_I \frac{S_I}{A_L} - \rho_L g \sin \theta \quad (27)$$

727 Presuming equality of pressure gradients in both phases, one can obtain a
 728 combined momentum equation:

$$F = \tau_{WG} \frac{S_G}{A_G} - \tau_{WL} \frac{S_L}{A_L} - \tau_I S_I \left(\frac{1}{A_G} + \frac{1}{A_L} \right) + g \sin \theta (\rho_L - \rho_G) = 0 \quad (28)$$

729 The next step is to express the forces engaged in the combined momentum
 730 equation. For the wall and interfacial shear stress, closure laws are needed.
 731 By applying the classical empirical correlations (Taitel and Dukler, 1976b),
 732 it follows that:

$$\tau_{WG} = \frac{f_G \rho_G U_G^2}{2} \quad (29)$$

733 and

$$\tau_{WL} = \frac{f_L \rho_L U_L^2}{2} \quad (30)$$

734 The interfacial shear stress reads:

$$\tau_I = f_I \frac{\rho_G (U_L - U_G)^2}{2} \quad (31)$$

735 Friction factors f_G, f_L, f_I can be expressed via the Blasius relations (Blasius,
736 1913):

$$f_L = C_L(Re_L)^{-n} = C \left(\frac{d_L U_L \rho_L}{\mu_L} \right) \quad (32)$$

737 and

$$f_G = C_G(Re_G)^{-m} = C \left(\frac{d_G U_G \rho_G}{\mu_G} \right) \quad (33)$$

738 where $C_L = C_G = 16$ and $m = n = 1$ for laminar flow ($Re < 2000$), whereas
739 $C_L = C_G = 0.046$ and $m = n = 0.2$ for turbulent flow ($Re > 2000$). Following
740 Chakrabarti et al. (2005), the friction factor at the interface is taken equal
741 to the friction factor of the faster-moving phase, *i.e.* $f_I = f_L$.

742 It follows that the combined momentum equation (Eq. 28) is a function
743 of liquid velocity, tube diameter, fluids properties and the hydraulic angle
744 β (via U_L, U_G and A_L, A_G). To assess the net of momentum of the system
745 (Eq. 28), both ways to compute shear stresses, *i.e.* produced via empirical
746 correlations (Eqs. 29 - 30), and determined analytically, (Eqs. 21 - 22), are
747 applied. The solution of the fully developed steady-state flow satisfies the
748 condition when the net of momentum is zero. Fig. 18 displays the variations
749 in the net of momentum (Eq. 28) depending on the hydraulic angle, where
750 τ^E (red dashed line) and τ^A (green dot-dashed line) refer to the empirical
751 correlations and analytical expressions of shear stress used for computations.
752 Filled rectangles identify the condition when $F=0$. Thereby, the hydraulic
753 angle corresponding to $F = 0$ will be assigned as the solution of the system.
754 The solution of the system can be expressed in terms of the liquid height
755 employing Eq. 1 and will be analysed in section 4.4.

756 4.2. Total Energy Minimization

757 The main idea of the energy minimization concept suggests that any
758 natural system stabilizes to its minimum total energy. Applied to the studied
759 flow, one can suppose that any air-water flow will be arranged in such a way
760 as to minimize the energy to be transported. In particular, the air-water flow
761 arrangement can be expressed in terms of the height of the liquid phase in
762 the tube cross-section, which is correlated to the hydraulic angle β (Eq. 1).
763 Thus, our aim here is to express the total energy of the two-phase flow as a
764 function of β , then define the hydraulic angle which results in the minimum
765 total energy.

766 The total energy of the air-water flow E_T is composed of potential E_P ,
767 kinetic E_K and surface E_S energies. Considering the air-water flow with the

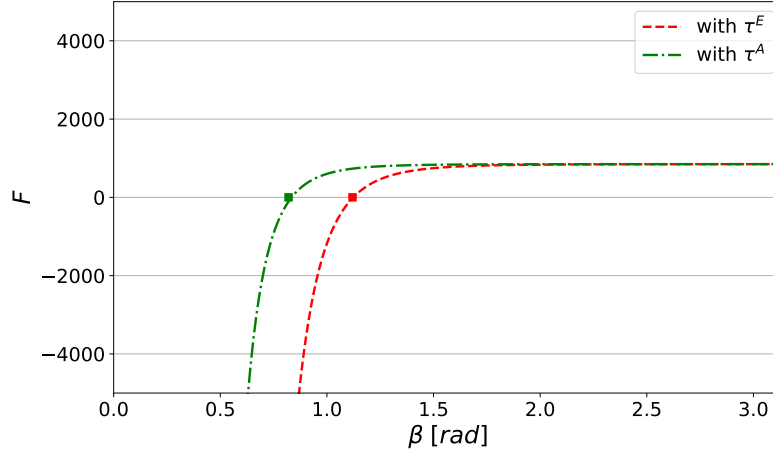


Figure 18: Net of momentum (F) (Eq. 28) calculated using τ^E (red dashed, Eqs. 29 - 30) and τ^A (green dot-dashed, Eqs. 21 - 22) for air-water two-phase flow in 3RFL with $d=69.85$ mm, $D = 0.84$ m, $\varphi_L = 0.05$, $\theta = 5^\circ$ and $f_R = 11.23$ opm. Filled squares mark the condition $F = 0$.

768 flat interface sketched in Fig. 17, the potential energy per unit length of the
 769 pipe is given as the sum of the potential energies of air and water phases:

$$E_P = E_{P_G} + E_{P_L} = A_L \rho_L g h_{cL} \cos \theta + A_G \rho_G g h_{cG} \cos \theta \quad (34)$$

770 where h_{cG} and h_{cL} are gas and liquid phases' gravity centres considered as:
 771 (Sharma et al., 2011):

$$h_{cG} = r \left[1 + \frac{4 \sin^3(\frac{\beta}{2})}{3(2\pi - \beta + \sin \beta)} \right] \quad h_{cL} = r \left[1 - \frac{4 \sin^3(\frac{\beta}{2})}{3(\beta - \sin \beta)} \right] \quad (35)$$

772 Analogously, the kinetic energy of the system per unit length of the pipe is
 773 the sum of the kinetic energies of air and water phases:

$$E_K = E_{K_L} + E_{K_G} = \frac{1}{2} A_L \rho_L U_L^2 + \frac{1}{2} A_G \rho_G U_G^2 \quad (36)$$

774 The surface energy of the two-phase flow per unit length of the pipe combines
 775 the surface energies at the gas-wall, liquid-wall and gas-liquid interfaces,
 776 considering that the latter is flat:

$$E_S = E_{S_{WL}} + E_{S_{GL}} + E_{S_{WG}} = S_L \sigma_{WL} + S_I \sigma_{GL} + S_G \sigma_{WG} \quad (37)$$

777 Here, σ_{WG} , σ_{GL} and σ_{WL} are wall-gas, gas-liquid and wall-liquid surface ten-
778 sions ($\sigma_{GL} = 72.8$ mN/m (Vargaftik et al., 1983), $\sigma_{WL} = 34$ mN/m (Schilling
779 et al., 2010)), respectively. The wall-gas surface tension σ_{WG} is neglected.
780 The total energy of the system per unit length of the pipe reads:

$$E_T = E_K + E_P + E_S \quad (38)$$

781 According to the energetic understanding of the problem, the solution of the
782 system is the β resulting in the minimum total energy $E_{T_{min}}$, *i.e.* $\beta_{min} =$
783 $\beta(E_{T_{min}})$.

784 Fig. 19 displays the variations in the total energy of the system (Eq. 38)
785 depending on the hydraulic angle. Here, the filled circle identifies the solution
786 corresponding to the minimum of the total energy. The resulting hydraulic
787 angle can be expressed in terms of the liquid height using the Eq. 1.

788 It is worth mentioning that the total energy of the system as a function
789 of hydraulic angle exhibits a table-top behaviour around the local minimum.
790 Thus, we have defined a region represented by the rectangle in Fig. 19, de-
791 limited by two values of β , *i.e.* β_{low} and β_{high} , for which $\beta_{low} < \beta < \beta_{high}$.
792 These values of β correspond to the hydraulic angle for which E_T varies by
793 25% concerning to its minimum. Once the ranges of the table-top region are
794 specified, the extreme values of the hydraulic angles, are expressed in terms
795 of the liquid height and compared to experimental results in section 4.4.

796 4.3. Combined Approach

797 In this section, we bring together the mechanistic approach along with
798 the energy minimization concept. Assuming the continuity of the pressure
799 gradient in the gas and in the liquid phase, and summing up the separate
800 momentum equations (24) and (25), one can derive the total pressure gradient
801 per unit length of the tube:

$$\frac{dP}{dx} = g \sin \theta (\rho_L \frac{A_L}{A_T} + \rho_G \frac{A_G}{A_T}) - \tau_{WL} \frac{S_L}{A_T} - \tau_{WG} \frac{S_G}{A_T} \quad (39)$$

802 One of the benefits of this mathematical operation is the liberation of the
803 combined momentum equation (39) from the shear stress at the interface τ_I ,
804 whose closure is usually a source of error. In order to combine the mecha-
805 nistic and energetic models, we follow Herri et al. (2017), where the authors
806 minimized the product of pressure gradient (Eq. 39) by the total energy of
807 the system (Eq. 38):

$$\min \left| \frac{dP}{dx} E_T \right| \quad (40)$$

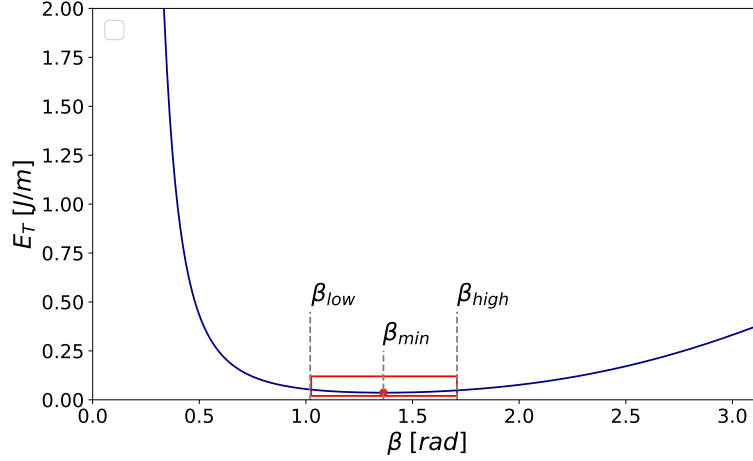


Figure 19: Total energy of air-water two-phase flow in 3RFL with $d=69.85$ mm, $D = 0.84$ m, $\varphi_L = 0.05$, $\theta = 5^\circ$ and $f_R = 11.23$ opm. The filled red circle marks the total energy's local minimum $E_{T_{min}}$. The red rectangle identifies the table-top behaviour around the local minimum (β_{min}) of the $E_T = f(\beta)$ function, where β_{high} and β_{low} identify the high and low limits.

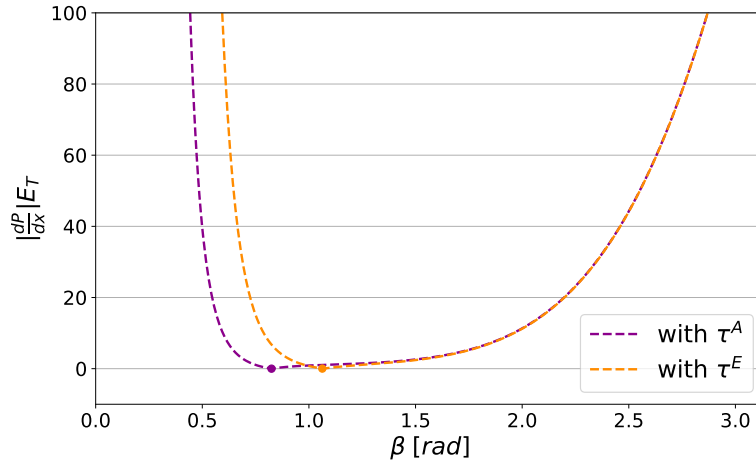


Figure 20: The product of pressure gradient exerted on the conduit cross section (Eq. 39) by the total energy of the system (Eq. 38) calculated using τ^E (orange dashed) and τ^A (purple dashed) shear stresses. Filled circles identify the local minima.

808 Fig. 20 presents the product of the pressure gradient by the total energy of
 809 the system as a function of β . Two approaches are employed to compute τ_{WG}
 810 and τ_{WL} in the Eq. (16): the empirical correlations τ^E (Eqs. 29 - 30), and the
 811 analytical expressions τ^A (Eqs. 21 - 22). The hydraulic angle corresponding
 812 to the local minimum (marked with filled circles) is recovered and expressed
 813 in terms of the liquid height following Eq. 1. Combined approach predictions
 814 are compared to the experimental measurements in the following section.

815 4.4. Comparison between experimental and modelling results

816 Fig. 21 shows the average liquid height \bar{h}_L as a function of the rocking
 817 rate f_R , and compares experimental results (black circles) and model predic-
 818 tions. The chosen configuration is: $d = 69.85$ mm, $\varphi_L = 0.05$, $\theta = 5^\circ$ and
 819 air-water flow. The boundaries of corresponding flow regimes are defined by
 820 vertical lines, as observed experimentally. Both mechanistic and combined
 821 model predictions are evaluated using for the wall shear stress empirical cor-
 822 relations τ^E (Eqs. 29 - 30) and analytical expressions τ^A (Eqs. 21 - 22).
 823 When employing the analytical correlation τ^A for the shear stress, the pre-
 824 dicted liquid height is underestimated for both the mechanistic (green solid
 825 line) and the combined (orange dot-dashed line) models, with respect to the
 826 scenario where τ^E is instead used, *i.e.* red solid line (mechanistic model) and
 827 purple dot-dashed line (combined model). Meanwhile, combined approach
 828 predictions employing τ^E (τ^A) situate close to the predictions of the mech-
 829 anistic model employing τ^E (τ^A), suggesting that the choice of the shear
 830 stress modeling plays an important role in the liquid film height prediction,
 831 even more than the choice of the modeling strategy itself (mechanistic or
 832 combined). However, the total energy minimization model (blue solid line),
 833 which by construction disregards the shear stress, provides an overestima-
 834 tion of the liquid film height predictions with respect to the mechanistic and
 835 combined approaches, regardless of the choice of the shear stress modeling.
 836 Nonetheless, when considering the confidence range of solutions (blue dot-
 837 ted lines) defined by the table-top region shown in Fig. 19, the lower limit
 838 predicts liquid film heights close to those of the mechanistic and combined
 839 approaches using τ^E .

840 The discrepancy observed between experimental results and mechanistic
 841 or combined models in the smooth interrupted (SI) and wavy-bubbly con-
 842 tinuous (WBC) flow regimes can be attributed to the inconsistency between
 843 the modeling assumption of stratified flow with flat interface and the actual
 844 characteristics of the flow. Indeed, the SI and WBC regimes typically exhibit

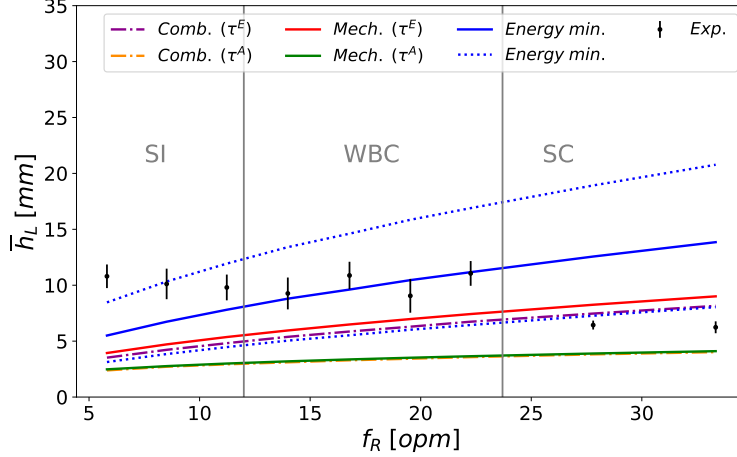


Figure 21: A comparison between liquid height predictions obtained from models, *i.e.* the mechanistic model with τ^A (green line) and τ^E (red line), energy minimization model (blue line) with the confidence range (blue dotted line), combined model with τ^A (purple dot-dashed line) and τ^E (orange dot-dashed line) and experimental results (black circles) considering air-water flow in the 3RFL with $d=69.85$ mm, $\varphi_L=0.05$, $\theta=5^\circ$ and various rocking rates.

845 a hump-shaped distribution of liquid along the flow (table 4). In contrast,
 846 the smooth continuous (SC) regime, characterized by its wall-clinging effect
 847 that promotes smooth interface and uniform distribution of liquid around the
 848 tube, matches more with the above-mentioned modeling assumption. Hence,
 849 experimental results for the SC regime align closely with mechanistic and
 850 combined models predictions. Finally, we can conclude that the total energy
 851 minimization model best predicts the experimental liquid heights, in partic-
 852 ular for the wavy-bubbly continuous flow. In addition, if confidence range is
 853 considered (blue dotted line), the liquid height predictions remain within the
 854 range of error bars for the all the experimental points, except the two limiting
 855 ones (very low and very large rocking frequency). However, noteworthy is
 856 that while the experimental liquid height is a constant or slightly decreasing
 857 function of the rocking frequency, the total energy minimization model - and
 858 also the mechanistic and the combined approach - predicts a growing trend
 859 of \bar{h}_L with f_R . This suggests that there is room for future improvements in
 860 the modeling strategy.

861 5. Conclusions

862 In conclusion, we have presented a new experimental system, the Rocking
863 and Rolling Ring Flow Loop, which can achieve controlled atmospheric flow
864 and different flow regimes. The advantages of the 3RFL are the simplicity of
865 fabrication, along with fast and simple operation and an accessible interior.
866 Besides, the geometry of the test section allows replicating flowlines of any
867 length. Another strength of the apparatus is flow initiation using mechanical
868 motion, rather than using pumping systems.

869 The transparency of the test section allowed flow regime analysis. For
870 the studied control parameters range, three flow regimes were identified,
871 such as smooth interrupted, smooth continuous and wavy-bubbly continu-
872 ous (Fig. 10). Air-water flow behaviour in the 3RFL showed similarities with
873 flow through the coiled tubes in terms of asymmetry of the flow in the ra-
874 dial direction (for SC and WBC flow regimes), non-homogeneous air bubbles
875 distribution along the flow (for WBC flow) and wall-clinging effect (for SC
876 flow). Given that coiled tubes can be used for heat-exchange applications,
877 natural gas hydrates separation from wax and asphaltenes (Tian et al., 2022),
878 and food and drugs manufacturing, flow regimes characterization presented
879 in the current work enriches experimental data on this matter. Flow observa-
880 tions were arranged into flow regime maps to evaluate flow regime transition
881 criteria and the impact of system control parameters on the emergence of par-
882 ticular flow regimes (Fig. 11). It was found that flow regime transitions are
883 mainly attributed to the value of the Fr number. Given that Fr expresses
884 the ratio of centrifugal forces to gravity, we conclude that competition be-
885 tween these two effects gives the resulting flow regime (Fig. 12).

886 Three models were selected to predict the average liquid height of the
887 air-water flow in the 3RFL: mechanistic, total energy minimization and a
888 combined approach. Analytical expressions for the shear stress were devel-
889 oped from the velocity profiles of liquid and gas. These expressions have been
890 employed as closure relations in the modeling approaches, and the resulting
891 liquid height have been compared to the case of empirical shear stress cor-
892 relations. Among those three employed modeling strategies, we have found
893 that the total energy minimization model best compares to the experimental
894 liquid height (Fig. 21).

895 Future work will concentrate on the parallel evolution of the complexity
896 of the experimental system and modeling. Improvements in experimental
897 research will involve advancing the experimental setup by introducing addi-

898 tional elements such as the oil phase and/or solid particles, implementing
899 pressurization, and establishing temperature control. These enhancements
900 will enable the development of a multi-instrumental flow loop for crystalliza-
901 tion experiments.

902 **References**

- 903 Akagawa, K., Kono, M., Sakaguchi, T., Nishimura, M., 1971. Study on
904 distribution of flow rates and flow stabilities in parallel long evaporators.
905 Bulletin of JSME 14, 837–848.
- 906 Amaravadi, S., 1994. The effect of pressure on two-phase zero-net liquid flow
907 in inclined pipes, in: SPE Annual Technical Conference and Exhibition,
908 OnePetro.
- 909 Balakin, B.V., 2010. Experimental and theoretical study of the flow, aggre-
910 gation and deposition of gas hydrate particles. Doctoral Dissertation, The
911 University of Bergen .
- 912 Banerjee, S., Rhodes, E., Scott, D.S., 1969. Studies on cocurrent gas-liquid
913 flow in helically coiled tubes. i. flow patterns, pressure drop and holdup.
914 The Canadian Journal of Chemical Engineering 47, 445–453.
- 915 Barnea, D., Taitel, Y., 1992. Structural and interfacial stability of multiple
916 solutions for stratified flow. International journal of multiphase flow 18,
917 821–830.
- 918 Barnea, D., Taitel, Y., 1994. Interfacial and structural stability of separated
919 flow. International journal of multiphase flow 20, 387–414.
- 920 Blasius, H., 1913. Das aehnlichkeitsgesetz bei reibungsvorgängen in
921 flüssigkeiten, in: Mitteilungen über Forschungsarbeiten auf dem Gebiete
922 des Ingenieurwesens. Springer, pp. 1–41.
- 923 Chakrabarti, D.P., Das, G., Ray, S., 2005. Pressure drop in liquid-liquid two
924 phase horizontal flow: Experiment and prediction. Chemical Engineering
925 & Technology 28, 1003–1009.
- 926 De Almeida, V., Serris, E., Lavalle, G., Cameirão, A., Herri, J.M., Abadie, E.,
927 Lesage, N., Fidel Dufour, A., 2023. Mechanisms of hydrate blockage in oil-
928 water dispersions based on flow loop experiments. Chemical Engineering
929 Science 273, 118632.

- 930 Dean, W.R., 1927. Xvi. note on the motion of fluid in a curved pipe. The
931 London, Edinburgh, and Dublin Philosophical Magazine and Journal of
932 Science 4, 208–223.
- 933 Eustice, J., 1911. Experiments on stream-line motion in curved pipes. Pro-
934 ceedings of the Royal Society of London. Series A, Containing Papers of a
935 Mathematical and Physical Character 85, 119–131.
- 936 Fidel-Dufour, A., Gruy, F., Herri, J., 2005. Experimental characterization
937 and modelling of the rheological properties of methane hydrate slurries
938 during their crystallisation in a water in dodecane emulsion under laminar
939 flowing. Chemical Engineering Science 61, 505–515.
- 940 Garcia, F., Garcia, R., Padrino, J., Mata, C., Trallero, J., Joseph, D., 2003.
941 Power law and composite power law friction factor correlations for laminar
942 and turbulent gas-liquid flow in horizontal pipelines. International Journal
943 of Multiphase Flow 29, 1605–1624.
- 944 Herri, J.M., Sum, A.K., Cameirao, A.A., Bouillot, B., 2017. Modeling non-
945 equilibrium crystallization of gas hydrates under stratified flow conditions,
946 in: 9 th International Conference on Gas Hydrates-ICGH9.
- 947 Kaji, M., Nakanishi, S., Mori, K., Kume, M., Moriya, T., 1984. Study
948 on dryout in helically coiled steam generating tubes, 1. comparison of
949 experimental results between coiled and straight tubes. Japan 50.
- 950 Kelland, M.A., Grinrød, A., Dirdal, E.G., 2015. Novel benchtop wheel loop
951 for low dosage gas hydrate inhibitor screening: comparison to rocking cells
952 for a series of antiagglomerants. Journal of Chemical & Engineering Data
953 60, 252–257.
- 954 Kinnari, K., Hundseid, J., Li, X., Askvik, K.M., 2015. Hydrate management
955 in practice. Journal of Chemical & Engineering Data 60, 437–446.
- 956 Kinnari, K., Labes-Carrier, C., Lunde, K., Hemmingsen, P.V., Davies, S.R.,
957 Boxall, J.A., Koh, C.A., Sloan, E.D., 2008. Hydrate plug formation pre-
958 diction tool—an increasing need for flow assurance in the oil industry. In:
959 Proceedings of the 6th International Conference on Gas Hydrates (ICGH
960 2008) .

- 961 Landman, M.J., 1991. Non-unique holdup and pressure drop in two-phase
962 stratified inclined pipe flow. *International journal of multiphase flow* 17,
963 377–394.
- 964 Lee, H., Al-Sarkhi, A., Pereyra, E., Sarica, C., Park, C., Kang, J., Choi,
965 J., 2013. Hydrodynamics model for gas–liquid stratified flow in horizontal
966 pipes using minimum dissipated energy concept. *Journal of Petroleum*
967 *Science and Engineering* 108, 336–341.
- 968 Melchuna, A.M., 2016. Experimental study and modeling of methane hy-
969 drates cristallization under flow from emulsions with variable fraction of
970 water and anti-agglomerant. Ph.D. thesis. Doctoral dissertation, Univer-
971 sité de Lyon.
- 972 Murai, Y., Yoshikawa, S., Toda, S.i., Ishikawa, M.a., Yamamoto, F., 2006.
973 Structure of air–water two-phase flow in helically coiled tubes. *Nuclear*
974 *engineering and design* 236, 94–106.
- 975 Nusselt, W., 1916. Die oberflächenkondensation des wasserdampfes. *VDI-Zs*
976 60, 541.
- 977 Ouyang, L.B., Aziz, K., 1996. Steady-state gas flow in pipes. *Journal of*
978 *Petroleum Science and Engineering* 14, 137–158.
- 979 Pham, T.K., Cameirao, A., Melchuna, A., Herri, J.M., Glénat, P., 2020.
980 Relative pressure drop model for hydrate formation and transportability
981 in flowlines in high water cut systems. *Energies* 13, 686.
- 982 Sa, J.H., Melchuna, A., Zhang, X., Morales, R., Cameirao, A., Herri, J.M.,
983 Sum, A.K., 2019. Rock-flow cell: an innovative benchtop testing tool for
984 flow assurance studies. *Industrial & Engineering Chemistry Research* 58,
985 8544–8552.
- 986 Schilling, M., Bouchard, M., Khanjian, H., Learner, T., Phenix, A., Rivenc,
987 R., 2010. Application of chemical and thermal analysis methods for study-
988 ing cellulose ester plastics. *Accounts of chemical research* 43, 888–896.
- 989 Sharma, A., Al-Sarkhi, A., Sarica, C., Zhang, H.Q., 2011. Modeling of
990 oil–water flow using energy minimization concept. *International Journal*
991 *of Multiphase Flow* 37, 326–335.

- 992 Sum, A.K., Koh, C.A., Sloan, E.D., 2009. Clathrate hydrates: From labora-
993 tory science to engineering practice. *Industrial & Engineering Chemistry*
994 *Research* 48, 7457–7465.
- 995 Taitel, Y., Barnea, D., 1990. Two-phase slug flow. *Advances in heat transfer*
996 20, 83–132.
- 997 Taitel, Y., Dukler, A.E., 1976a. A model for predicting flow regime transi-
998 tions in horizontal and near horizontal gas-liquid flow. *AIChE journal* 22,
999 47–55.
- 1000 Taitel, Y., Dukler, A.E., 1976b. A model for predicting flow regime transi-
1001 tions in horizontal and near horizontal gas-liquid flow. *AIChE journal* 22,
1002 47–55.
- 1003 ISO/IEC, 2008. Uncertainty of measurement — Part 3: Guide to the ex-
1004 pression of uncertainty in measurement (GUM:1995) . 2008(E) ed., In-
1005 ternational Organization for Standardization, Geneva, Switzerland. URL:
1006 <https://www.iso.org/standard/50461.html>.
- 1007 Thibault, D., Munoz, J.M., Liné, A., 2015. Multiple holdup solutions in lami-
1008 nar stratified flow in inclined channels. *International Journal of Multiphase*
1009 *Flow* 73, 275–288.
- 1010 Tian, J., Xiao, X., Yang, L., Liu, C., Guo, L., 2022. Separation mechanism
1011 and dynamics characteristics of natural gas hydrate by helically coiled
1012 tube. *Heat and Mass Transfer* 58, 1459–1471.
- 1013 Ullmann, A., Zamir, M., Gat, S., Brauner, N., 2003. Multi-holdups in co-
1014 current stratified flow in inclined tubes. *International journal of multiphase*
1015 *flow* 29, 1565–1581.
- 1016 Vargaftik, N., Volkov, B., Voljak, L., 1983. International tables of the surface
1017 tension of water. *Journal of Physical and Chemical Reference Data* 12.
- 1018 Xiao, J., Shonham, O., Brill, J., 1990. A comprehensive mechanistic model
1019 for two-phase flow in pipelines, in: *SPE Annual Technical Conference and*
1020 *Exhibition, OnePetro*.
- 1021 Zhu, G., Yang, X., Jiang, S., Zhu, H., 2019. Intermittent gas-liquid two-
1022 phase flow in helically coiled tubes. *International Journal of Multiphase*
1023 *Flow* 116, 113–124.